



The design and analysis of a high-production mini-computer systém for regridding digital terrain elevation matrices

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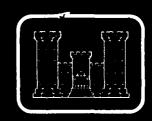
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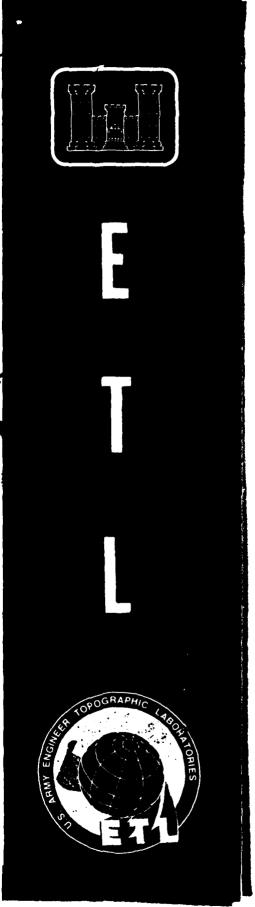
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UNCLASSIFIED SECURITY CLASSIFICATION OF THIS PAGE (When Date Entered) READ INSTRUCTIONS REPORT DOCUMENTATION PAGE BEFORE COMPLETING FORM 2. GOVT ACCESSION NO. 3. RECIPIENT'S CATALOG ETL/0240 TYPE OF REPORT & P THE DESIGN AND ANALYSIS OF A HIGH-PRODUCTION CONTRACT REPORT MINI-COMPUTER SYSTEM FOR REGRIDDING DIGITAL 6. PERFORMING ORG. REPORT NUMBER FIFVATION MATRICES B. CONTRACT OR GRANT NUMBER(a) George C./Stockman, Russell C./Smith, I-Lok DAAK78-80-C-0022 Chang PERFORMING ORGANIZATION NAME AND ADDRESS PROGRAM ELEMENT, PROJECT, TASK AREA & WORK UNIT NUMBERS L.N.K. Corp<del>oratio</del>n 302 Notley Court Silver Spring, Md. 20904 12. REPORT-DATE October 1980 U.S.Army Engineer Topographic Laboratories NUMBER OF PAGES Fort Belvoir, Virginia 22060 14. MONITORING AGENCY NAME & ADDRESS(II different from Controlling Office) 15. SECURITY CLASS. (of this report) UNCLASSIFIED 15a. DECLASSIFICATION/DOWNGRADING 16. DISTRIBUTION STATEMENT (of this Report) Approved for Public Release; Distribution Unlimited 17. DISTRIBUTION STATEMENT (of the abstract entered in Block 20, if different from Report) 18. SUPPLEMENTARY NOTES 19. KEY WORDS (Continue on reverse side if necessary and identify by block number) Digital Terrain Elevation Matrices

20. ABSTRACT (Continue on review side if recessary and identify by block number)

This report studies a new algorithm for the regridding and transformation of Digital Terrain Elevation Matrices. The new algorithm uses sequential accesses to mass storage devices rather than the random methods used by the software system currently installed at the Defense Mapping Agency. Due to the simplicity of the new algorithm, minicomputers can be used in place of a large mainframe computer. Four potential minicomputer systems are examined. Benchmark test results are given which show the feasibility of minicomputer use. Recommendations are

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# PREFACE

This document was generated under Contract DAAK 70-80-C-0022 for the U.S. Army Engineer Topographic Laboratories, Fort Belvoir, Virginia, 22060, by L.N.K. Corporation, 302 Notley Court, Silver Spring, Maryland and submitted as ETL-0240. The Contract Officer's Representative was William Edward Opalski. The authors thank Mr. Opalski and also Mr. Arthur Noma and Dr. Clifford Kottman of the Defense Mapping Agency Hydrographic/ Topographic Center for their helpful comments on the draft of this report.

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# Executive Summary

The objective of this report is to:

- present an algorithm for regridding and transformation of digital terrain elevation matrices that will efficiently run on a minicomputer,
- (2) benchmark trans ormation and I/O times on four candidate minicomputer systems,
- (3) make recommendations as to which minicomputer systems will perform most efficiently, and
- (4) recommend modifications to DMAHTC current Mosaicking and Regridding Software System (MARS).

The motivation for the study effort came from the realization that the MARS system, which is implemented on a UNIVAC 1100/81 mainframe, has bottlenecks that result from certain operating system constraints. In looking for a solution to this problem it became apparent that state-of-the-art minicomputer systems, particularly the 32 bit machines, could perform as well or better than the UNIVAC 1100/81, especially if the regridding and transformation functions were performed in a sequential manner rather than the current random manner. A new algorithm was designed with a view toward installing it on a "fast" minicomputer. The new algorithm could be implemented on the UNIVAC 1100/81, however, it would not achieve the same efficiency as it will on a suitable minicomputer.

Section 2 describes the new algorithm and its refinement. The new algorithm rearranges the regridding and transformation task so that sequential accessing methods to mass storage devices can replace the current

random access methods. Due to the resulting simplification of the processing needs the new algorithm can be installed on a minicomputer, allowing easy and inexpensive expansion should there be a future increase in workload.

Section 3 examines the specifications of minicomputer systems which could perform the new algorithm efficiently enough to compete with the UNIVAC 1100/81. Both 16 bit and 32 bit minicomputers are examined. A comparison of relative costs is made. Special hardware options which can significantly improve execution times are noted.

Benchmark tests were run on a subset of the minicomputers presented in Section 3 in order to determine if preliminary estimates of their speeds were correct. In Section 4 the results of these tests are given. I/O transmission speeds are shown to be more than sufficient for the implementation of the new algorithm. The speed at which a minicomputer could perform a computebound point-to-point transformation, necessary for the regridding task, shows that the fastest (and most expensive) minicomputers would be necessary if each point in the Digital Terrain Matrix were to be rigorously transformed. However, only a small portion of the points are rigorously transformed by the current software used by DMA. Under these circumstances, all the minicomputers examined can be used for the new algorithm.

Scetion 5 presents an overview of the study, conclusions, and recommendations. General conclusions regarding the transportation of the software from the UNIVAC 1100/81 to a minicomputer, including estimates of costs, are given. The recommendation is made that a 32 bit minicomputer (PERKIN-ELMER 3240) be chosen for the implementation of the new algorithm. This recommendation is based on the ease of implementation possible with the larger address space of a 32 bit computer when compared to that of a 16 bit computer and the capability of a 32 bit computer in handling future DMA needs.

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#### INTRODUCTION

The Defense Mapping Agency Hydrographic/Topographic Center (DMAHTC) has a requirement to convert a large photogrammetric source database to digital terrain elevation matrices. This conversion is currently achieved in large part by scanning raw photogrammetric data with specialized hardware (Universal Automatic Map Compilation Equipment or UNAMACE), the output of which is a matrix of elevation values (Digital Terrain Matrix or DTM). DTM's are combined to form 1 squares and stored in a digital database using DMAHTC Standard Format. The process of combining, called mosaicking, involves the regridding and transformation of the DTM's. This is currently accomplished using a complex system of software called the Mosaicking And Regridding System (MARS) developed and implemented at DMAHTC by L.N.K. Corporation in 1978.

MARS, designed to run in batch mode on a UNIVAC 1100/81 computer, has been vital to DMA in handling the conversion of UNAMACE data. However, after working at DMAHTC with the system on a daily basis for two years and gaining an intimate knowledge of the operator interface, machine resource requirements and wall clock time necessary for the regridding and transformation process, L.N.K. determined that some portions of the MARS system were in effect bottlenecks. These bottlenecks are due to constraints imposed by the UNIVAC operating system. In particular, the limiting of the memory address space leads to a fragmentation of the data being processed, thus excessive random accesses to mass storage devices are required.

After collection of statistics on the regridding and transformation process and upon closer examination of both the details of the process and the capabilities of state-of-the-art minicomputers, L.N.K. estimated that the regridding and transformation task could be performed on a dedicated

minicomputer more efficiently than on the UNIVAC 1100/81. In addition, the implementation of a "MiniMARS" would allow for easy expansion to handle any increase in processing needs simply by adding to the number of minicomputers used for the task.

- L.N.K. therefore proposed a study effort to:
- Develop a new algorithm for the regridding and transformation process which would significantly decrease the number of random accesses to mass storage devices,
- (2) Examine a selection of minicomputer systems and prove they could efficiently and effectively perform the new algorithm,
- (3) Recommend DMAHTC purchase any one of four select systems, and
- (4) Recommend modifications to the current MARS system which could improve throughput on the UNIVAC 1100/81. These modifications are not an implementation of the new algorithm, but an optimization of the code used in the current MARS.

In the study benchmark tests were devised and implemented on a number of minicomputer systems to determine possible transformation and I/O times for the regridding and transformation task. Using the results from these tests L.N.K. confirmed that state-of-the-art minicomputers (PERKIN-ELMER 3240, DATA GENERAL ECLIPSE S/250, PDP 11/44) can compete with large mainframes such as the UNIVAC 1100/81 when the minicomputers are dedicated to the task at hand. The details of the algorithm, tests, and recommendations are included in this report.

#### ALGORITHMS

#### 2.1 The Proposed Algorithm

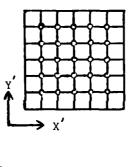
Universally, the regridding and transformation task consists of

- (1) Definition and creation of a target coordinate system grid,
- (2) Input and transformation of input digital elevation data, and
- (3) Creation of the output model.

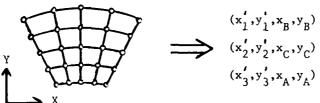
Regridding and transformation, normally performed using random access methods with the MARS software system, has been restructured in the new algorithm into a series of sequential file processing steps. Each step, due to simplicity, can be efficiently implemented on a minicomputer system.

The proposed new algorithm is a 4 step process. Initially the target coordinate system grid is defined. Each point in this grid (x',y') is transformed to the input model's coordinate system, thus producing a set of quadruples (x',y',x,y). These quadruples are then sorted according to the (x,y) coordinates. The sorted quadruples are now merged with the input model, interpolating elevation values for (x,y) as is currently done with the MARS system. The result of this step is a set of triples (x',y',z') which are in the input model's order. Therefore these triples are resorted according to the (x',y') coordinates, producing a file with the correct order for the output model. Figure 1 illustrates the steps of this process. Note that the transformation from one coordinate system to the other is considered to be done by a "black box", i.e. any transformation function can be used with this system, including those used by MARS.

An elementary version of the algorithm was implemented on a UNIVAC 1108 computer. Initially a small input model (20 x 20 points) was hand-created. A target coordinate system was defined as a small rotation and translation of the input coordinate system. A file of 400 quadruples (x',y',x,y) was created.



SELECT OUTPUT
COORDINATE SYSTEM,
PRODUCE OUTPUT GRID



TRANSFORM EACH POINT TO INPUT COORDINATE SYSTEM, CREATING QUADS

SORT QUADS ACCORDING TO (x,y), MERGE WITH INPUT FILE, INTERPOLATE, AND PRODUCE OUTPUT TRIPLES.

$$(x'_{3}, y'_{3}, z') \\ (x'_{1}, y'_{1}, z') \\ (x'_{2}, y'_{2}, z') \\ (x'_{3}, y'_{3}, z')$$

SORT TRIPLES ACCORDING TO (x',y').

z' z'

PRODUCE OUTPUT MOSAIC FILE FROM TRIPLES.

Figure 1. Flow diagram for initially proposed algorithm

The quadruple file was sorted according to the (x,y) coordinates using the UNIVAC system sort routine SORTSDF. The file of quadruples and the input model were then merged, interpolating new elevation values by using a simple four neighbor average. The output of this step (x',y',z') was sorted according to the (x',y') coordinates and then plotted. Figure 2 shows both the input model and the resulting output model. Numerical elevation values are represented by alphanumeric characters. It should be noted that in a real system no elevation data would be thrown away. In this case data was clipped only for uniformity of plot size.

The algorithm thus has been graphically shown to be correct. However on further analysis it was found that by increasing the size of the memory space and using in-core addressing methods the sort steps could be dropped, greatly increasing the throughput of the system. The refined algorithm is detailed below.

# 2.2 The Refined Algorithm

#### 2.2.1 NOTATION

As in the proposed system primes are used to indicate points in the output grid coordinates, such as (x',y'). Unprimed quantities are reserved for input grid coordinates, such as (x,y). T(x',y') or T(x',y',z) is the output grid point (x',y') transformed into the input grid coordinate system.

#### 2.2.2 REGRIDDING AND BINNING

As Figure 3 shows, output grid points will be transformed into the input Digital Terrain Matrix (DTM) coordinate system so that elevation values can be determined for each one by interpolation. Assuming an N  $\times$  N input DTM, every transformed grid point must lie in one of N + 1 "aisles" or bins. For a 1024  $\times$  1024 input DTM there are only 1025 bins.

2 ORIGINAL INPUT MODEL RS&T S QI TRANSFORMATION 8105501 2 1 8  $R = 30^{\circ}$ I Q S S Q I 8 2 1 1 1 T = (=8, -4)MODEL AFTER TRANSFORMATION TO OUTPUT COORDINATE SYSTEM The line segments at right angles enclose the same region in the two

Figure 2. Sample Input and Output of Initial MiniMARS Test

models. Note that due to inter-

polation the elevation values are slightly changed at region borders.

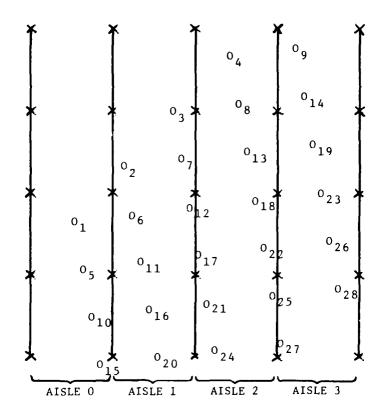


Figure 3. All output grid points will lie in one of N+1
"aisles" for an N X N input DTM.

#### 2.2.3 INTERPOLATION

During interpolation, the elevation of each output grid point  $(0_1,0_2,\ldots,0_{28}$  in Figure 3) will be determined from the elevations of only 4 points in the input DTM, which lie on only two profiles. Figure 4 shows the 4 "neighbors" used to compute the elevation at point T(x',y'). If the input grid points are never more than 128 meters apart at true scale a fraction of 6-bit precision for T(x',y') will yield 2 meter positional accuracy in the (x,y) space.

#### 2.2.4 COORDINATE CODING

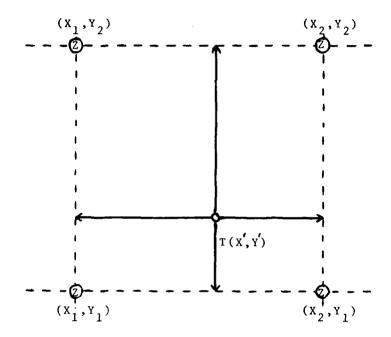
Using 16 bits overall and 6 bits for a fraction, T(x',y') = (x,y) will be coded as follows

$$\mathbf{x} \simeq \mathbf{D}_{\mathbf{x}} \mathbf{1}^{\mathbf{D}}_{\mathbf{x}} \mathbf{2} \cdots \mathbf{D}_{\mathbf{x}} \mathbf{10} \cdot \mathbf{F}_{\mathbf{x}} \mathbf{1}^{\mathbf{F}}_{\mathbf{x}} \mathbf{2} \cdots \mathbf{F}_{\mathbf{x}} \mathbf{6}$$
$$\mathbf{y} \simeq \mathbf{D}_{\mathbf{y}} \mathbf{1}^{\mathbf{D}}_{\mathbf{y}} \mathbf{2} \cdots \mathbf{D}_{\mathbf{y}} \mathbf{10} \cdot \mathbf{F}_{\mathbf{y}} \mathbf{1}^{\mathbf{F}}_{\mathbf{y}} \mathbf{2} \cdots \mathbf{F}_{\mathbf{y}} \mathbf{6}$$

The consequences of 2 meter accuracy at up to 128 meter spacing is a limit on the model size to  $1024 \times 1024$  if the above 16-bit coordinates are to be used. However, the above bit pattern can be varied as is needed. Using fewer fraction bits allows a larger DTM to be manipulated.

## 2.2.5 SAMPLING GRID GENERATION

The output grid points will be generated and transformed into the input coordinate space. During generation each point will be represented by a quadruple (x',y',x,y), where  $(x,y) \neq T(x',y')$ , which will immediately be placed in the correct aisle for later sequential merging with the input



ELEVATION AT T(X',Y') IS INTERPOLATED FROM THE ELEVATIONS AT  $(X_1,Y_1)$ ,  $(X_2,Y_1)$ ,  $(X_1,Y_2)$ , AND  $(X_2,Y_2)$ . IF INPUT SPACING IS LESS THAN OR EQUAL TO 128 METERS, A 6 BIT FRACTION WILL YIELD 2 METER ACCURACY.

Figure 4. Elevations of transformed output points are interpolated from elevations of input points.

DTM. The rough algorithm is as follows:

- (Al) Get input DTM specs from the header and define the output grid and transformation T.
- (A2) Generate and bin each point of the output grid
  - (A2.1) For each point (x',y') produce the quadruple (x',y',x,y) where (x,y) = T(x',y') and where  $x = D_x 1 D_x 2 \cdots D_x 10 \cdot F_x 1 F_x 2 \cdots F_x 6$  and  $y = D_y 1 D_y 2 \cdots D_y 10 \cdot F_y 1 F_y 2 \cdots F_y 6$
  - (A2.2) Place each quadruple (x',y',x,y) into aisle A which is  $D_{x1}D_{x}^{2}...D_{x10}$  in binary.

#### 2.2.6 IMPLEMENTATION

No aisle can receive more than  $1024\sqrt{2}$  quadruples (the square root value comes from the diagonal of the matrix) hence 8 times this (about 15000) bytes of storage are needed for each aisle. In main memory we can statically allocate 1025 blocks of size 25 quadruples (i.e. 200 bytes) each. When full, each 25 quadruple block will be output to a known track storing the appropriate aisle. There will thus be about  $2^{20}/25$  writes (about 40000). This will require 40000 x 43 ms average access time plus  $2^{23}$  bytes/(8x10<sup>5</sup> bytes/second transfer rate) or about 1730 seconds, approximately 1/2 hour. A refined algorithm will now be given which will reduce the number of disk writes, and hence the execution time, by half.

# 2.3 Further Analysis of the Refined Algorithm

An in depth analysis of the refined algorithm using data on off-the-shelf minicomputer systems is given on the following pages. Though the DATA GENERAL S/250 was used for the basis of the times given, all the machines examined in Section 3 have similar I/O speeds. Therefore the use of the DATA GENERAL times should not be construed as a recommendation of the S/250.

# 2.3.1 ASSUMPTIONS CONCERNING HARDWARE

The refined algorithm which follows refers to general specifications for high speed minicomputer systems, for example the DATA GENERAL S/250 or the PERKIN-ELMER 3240. Memory size necessary for efficient implementation of the algorithm should be at least 2<sup>18</sup> bytes (256K bytes). Peripheral equipment also needed include two independent disk drives (i.e., capable of performing operations simultaneously) and two 1600BPI 9-track tape drives. The disk drives assumed each have five surfaces and 815 cylinders. Each track (intersection of one surface with a cylinder) contains 24 sectors of 512 bytes. The average access time of the disk drives is an important parameter and should be close to the 43 millisecond access time of the DATA GENERAL drives. The tape drives, though not as important with respect to speed, are assumed to be capable of reading and writing at 75 inches/second.

Step 1. Generate output grid, transform, and "aisle sort" to disk.

# Algorithm

Read header of input DTM and define output grid.

Generate and transform output grid points (x',y') to get quads (x',y',x,y) with (x,y) = T(x',y').

Output quads in blocks of 512 bytes, or 64 quads, to one of 256 cylinders on disk according to first 8 bits of x. (i.e. each cylinder would store 4 aisles of data)

# Main Memory Data Structures

256 block buffers @ 512 bytes each (128K bytes)

3 output buffers @ 512 bytes each (1.5K bytes)

256 block headers @ 4 bytes each (1K bytes)

#### Disk Structure

bin K stored on cylinder K,  $0 \le K \le 255$ 

K selected as first 8 bits of x in quad

60,000 bytes per cylinder allows 7,000 quads max per 4 aisles

# Timing for 2<sup>20</sup> points assuming no I/O overlap

Transform: 3 to 45 minutes

Output: 8 Mbvtes/512 = 16K blocks

16K blocks x 50 x  $10^{-3}$  seconds each  $\approx$  800 seconds = 13 minutes

Step 2. Collate quads with input DTM profiles and sort on x' on output

#### Algorithm

Read first 5 input DTM profiles.

Read next block of quads in one of 4 aisles between the 5 profiles.

For each quad (x',y',x,y) use (x,y) to interpolate z'. Then place (x',y',z') in output block buffer according to the first byte of x'. When the current 4 aisles are exhausted move on to the next 4 input DTM profiles.

# Main Memory Data Structures

Tape: 10 input profile buffers @ 2,050 bytes each (20K bytes)

256 block buffers @ 512 bytes each (128K bytes)

256 block headers @ 4 bytes each (1K bytes)

Disk out: 3 output buffers @ 512 bytes each (1.5K bytes)

Disk in: 3 input buffers @ 2,048 bytes each (6K bytes)

#### Disk Structure

Input: quad file as in Step 1 output

Output triples

bin K stored on cylinder K, 0 < K < 255

K selected as first byte of x'

85 triples per 512 byte block, hence 10,200 triples per cylinder

this allows 10 profiles @ 1,020 points each; typically only

4 will exist since  $\mathbf{x}'$  has only 10 bits of integer

# Timing for $2^{20}$ points assuming no I/O overlap

input from tape 1000 blocks @ 2" each

2000" @ 75ips = 30 seconds

input from disk<sub>1</sub>

4K blocks (of 2048 bytes) x 50 x  $10^{-3}$  seconds each = 200 seconds output to disk<sub>2</sub>

12K blocks (of 512 bytes) x 50 x  $10^{-3}$  seconds = 600 seconds

main memory processing (estimated interpolation time)

≈ 180 seconds

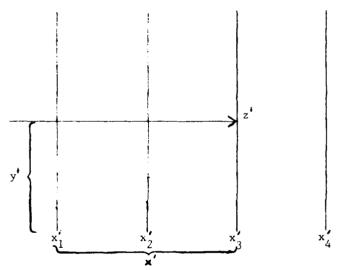
TOTAL TIME = 1,000 seconds

# Step 3. Final Model Output

# Algorithm

Read entire next bin (cylinder) of triples and assemble up to 10 profiles of z' values by selecting the profile with x' and the point position with y'.

Repeat for all bins.



Place z' in position addressed by x' and y'

# Main Memory Data Structures

output buffers for output tape

20 profiles x 1,500 points x 2 bytes each = 60,000 bytes

for 2 sets of buffers

input buffers for triples

2 buffers @ 2,048 bytes each

Timing assuming no overlap for 2<sup>20</sup> points

writing output tape = 30 seconds

in core = 200 seconds (very conservative estimated time)

input of 3K blocks of 2,048 bytes each

 $3K \times 50 \times 10^{-3}$  seconds = 150 seconds

TOTAL TIME ≈ 380 seconds

#### TOTAL TIMES FOR THE 3 STEPS

Step 1. 17 to 58 minutes\* (clear bottleneck)

Step 2. 16 minutes

Step 3. 7 minutes

TOTAL 40 to 80 minutes

\*high value for rigorous point-to-point transformation; low value for maximum interpolation

Figures 5 and 6 illustrate the refined algorithm. The sort steps have essentially been eliminated through the use of direct addressing methods (both main memory and disk). The refined algorithm requires a larger (256K =  $2^{18}$ ) memory space than is normally directly addressable by a 16 bit minicomputer.

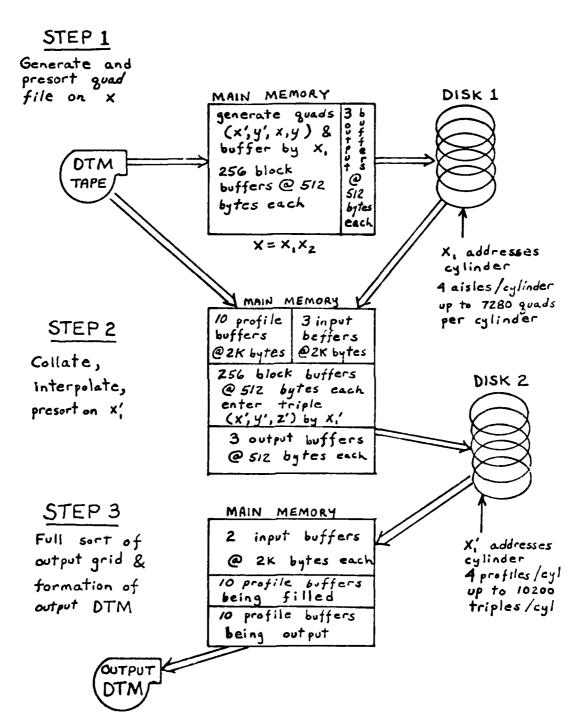


Figure 5. Flow diagram for the refined MiniMARS algorithm

MAIN DISK MEMORY 1600 BPI 5 surfaces 815 cyls 256kbytes 24 sectors/track 75 inches/sec 512 bytes/sector 43 MSEC avg access MODEL Generate output grid, aisle-sorted transform, & aisle sort. OUTPUT FILE of INPUT FILE STEP 1 256 block buffers @ 512 ≤ 8M quads bytes each, 256 block KEY = CYL# =headers @ 4 bytes each first byte of X from  $(x^1, y^1, x, y)$ 3 512 byte buffers for disk output Interpolation sequential presorted MODEL INPUT FILE of OUTPUT INPUT FILE & presort of triples. FILE of STEP 2 10 input profile of aislesequential buffers @ 2050 bytes **¥**8M sorted quads by x & y each, 256 block buffers triples KEY = CYL# @ 512 bytes each = first 256 block headers @ byte of x1 4 bytes each from (x1, 3 input buffers for  $y^1, z^1$ ) DISK 1 @ 2048 bytes 3 output buffers for DISK2 @ 512 bytes Assemble output sequential MODEL INPUT FILE OUTPUT model profiles. STEP 3 FILE 2 input buffers of presorted @ 2048 bytes each triples 20 output buffers @ 3000 bytes each

Figure f. Peripheral flow diagram for the refined MiniMARS algorithm

#### HARDWARE

The refined regridding and mosaicking process requires a fair amount of main memory (256K bytes) in order for it to perform fast enough to be more efficient than the methods used in the MARS software system on the UNIVAC 1108. The basic requirements of the minicomputer hardware system are:

- 1) 256K byte main memory (minimum)
- 2) Floating point instructions (hardware, not software interpreted)
- 3) 2 fast disk drives (average access time approximately 45 milliseconds), capacity of each drive at least 50M bytes
- 4) Two 1600 bpi 9 track tape drives, 75 inch per second read/write speed (or faster).

In addition, some method of producing hardcopy output for monitoring the regridding and mosaicking process, such as a printing console terminal, and software comprising a FORTRAN compiler and text editor are essential.

Table 1 gives a price breakdown of 4 off-the-shelf minicomputer systems which meet these requirements. The prices stated are based on the formal manufacturer's quotes contained in Appendix B. The formal quotes, compiled by sales representatives of the companies DATA GENERAL, PERKIN-ELMER, and DIGITAL EQUIPMENT contain certain discrepencies in system configuration which are outlined on the quotation sheets. The discrepencies can increase the bottom line costs for the systems by as much as 20%. Table 1 should be used as the cost guideline in place of the Quotation sheets. All prices in Table 1 reflect the manufacturer's GSA discount, 15% for DATA GENERAL and DIGITAL EQUIPMENT, 21% for PERKIN-ELMER.

The systems examined were felt to be adequate for the task at hand since each could perform the approximate transform on on a set of points

with sufficient speed to compete with the performance of the UNIVAC 1108. DIGITAL EQUIPMENT Corporation's PDP11 systems were not studied as thoroughly as the other three systems, however, because it was found that they could not meet the timing specifications if rigorous transformation was to be performed on more than a small percentage (~1%) of a given set of points. Based on manufacturer's literature the arithmetic logic is much slower than that of the other systems studied, but they can still perform to specs provided that few rigorous transformations are required (It should be noted that the current MARS system rigorously transforms only about 0.5% of the set of points, the remainder being approximately transformed). The sections following provide a closer look at the DATA GENERAL Eclipse S/250 and the PERKIN-ELMER 3220 and 3240 minicomputers. Conclusions and recommendations are given in Section 5.

#### 3.1 The DATA GENERAL Eclipse S/250

The DATA GENERAL Eclipse S/250 is a general purpose 16 bit minicomputer with a large and varied instruction set. Its optional floating point processor has the capability of 64 bit precision, necessary for the transformations used and can preserve least significant digit accuracy over many computations. The S/250 also has a Writable Control Store option which could prove to be highly useful for improving the speed of certain time intensive computations. With this option installed, frequently used functions or subroutines (such as the trigonometric functions SIN, COS, and TAN) could be coded to work much faster than that possible with assembly language. The resulting increase in execution speed could be significant (see Section 4). In general, the ability to microcode a computer allows one to tailor the hardware to specific needs.

DATA GENERAL manufactures its own disk drives. The drives considered have a capacity of about 50M bytes broken down into 5 surfaces each with 815 tracks. Each track contains 24 sectors of 512 bytes. Though the desired disk addressing would be in powers of two, it is not felt that the effect of non-power of two addressing present on these drives will be significant. These disk drives are high speed with an average access time of 43 milliseconds.

The DATA GENERAL tape drives are industry compatible 9 track 800/1600 bpi 75 inch/second, capable of working with the high speed Burst Multiplexor Channel option of the S/250. The Burst Multiplexor Channel permits very fast direct memory access for both the tape and disk drives. Due to its relative low cost (~2% of total system cost) it is felt that this option should be included if the S/250 is selected fo the MiniMARS project.

One interesting aspect of the S/250 is the optional built-in array processor. The regridding and transformation task lends itself to implementation on an array processor since the transformation is to be performed

on a set of points, not unlike operating with a vector of elevation values. This processor, installed in the main CPU cabinet, will recognize special instructions which allow the same operation to performed on a set of values. The possible increase in execution speed is similar to that obtained with the Writable Control Store. The array processor permits a floating point precision of 32 bits, adequate for many parts of the regridding and mosaicking task.

## 3.2 The PERKIN-ELMER 3220 and 3240

The PERKIN-ELMER 3220 minicomputer and its upgrade, the 3240, are science oriented 32 bit computers. Both machines offer a floating point processor option with 64 bit precision. The major difference between the PERKIN-ELMER floating point processor and those of other manufacturers (including DATA GENERAL) is the rounding method used after performing a floating point operation. Called R\* (R-STAR) rounding, the method can guarantee results at least as accurate as those obtained by truncation or one way rounding over long series of computations. In actual fact, R\* results are usually more accurate and could prove useful for the transformation software.

Both the 3220 and 3240 have multiway memory interleaving which can increase the apparent memory speed with a resultant decrease in execution time. The PERKIN-ELMER 3240 has a Writable Control Store option which can cause significant improvement in execution speed, to the extent that transformation times on the 3240 with microcoded transcendental functions are comparable to those obtained from a UNIVAC 1108 (see Section 4).

The disk drives used by PERKIN-ELMER are supplied by Control Data Corp. They are similar to ... DATA GENERAL drives in layout but have a slightly higher capacity (67M bytes) and slightly faster access time (38ms). The higher speed may contribute about a 6% decrease in the I/O times when compared to those of DATA GENERAL. The industry compatible tape drives which come with the PERKIN-ELMER machines (as configured) are virtually identical to those of DATA GENERAL.

PERKIN-ELMER minicomputers do not have a built-in array processor option.

Instead, the array processors offered by PERKIN-ELMER are in free standing cabinets and are produced by Floating Point Systems. These processors come in a variety of configurations including models with either 32 or 64 bit precision.

Certain parts of the transformation algorithms require a high degree of precision. Should the array processor option be desired, selecting one with 64 bit precision would allow more of the transformation algorithm to be used in a vector of values at one time than if a 32 bit precision model is chosen. The difference in cost between the 32 bit and 64 bit Floating Point Systems array processors would have to be taken into consideration before any firm decision could be made (FPS recently announced their 64 bit array processor. The 32 bit processor is in the \$100K range. The 64 bit processor is nearly double that.).

Table 1.

COMPARATIVE PRICES

		DATA GENERAL S/250	PERKIN-ELMER 3220	PERKIN-ELMER 3240	DEC 11/44
ITEM		5/250			11/
CPU + 256K Byte Memory		\$34,425	\$28,440	\$87,690	\$23,545
Floating Point roc.		\$5,266	\$4,424	\$7,505	\$2635
High Speed	(1)	\$18,530	\$12,008	\$12,008	\$21,845
Disk Drive	(2)	\$18,530	\$12,008	\$12,008	\$16,405
Tape Drive	(1)	\$13,175	\$15,089	\$15,089	\$17,170
High Speed	(2)	\$9,605	\$7,603	\$7,603	\$10,880
Printer		\$2,252	\$3,476	\$3,476	\$1445
Other: Cache	•	(cabinet) \$2,600 (BMC) \$2,678	(cabinet) \$869 (channels) \$2,765	(channels) \$2,765 (cache) \$5,925	(cabinet \$1105 (expansion \$2720
Cabinets, CI	lock ce,e	, (cache)	(cache) \$2,765 (power) \$1,343 (clock) \$711		(interface \$731 (cable) \$51 (clock) \$697
Software		\$4,400	\$12,600	\$12,600	\$8800
TOTAL		\$115,031	\$104,101	\$166,669	\$107,978

\*NOTE\* The PERKIN-ELMER software costs reflect their pricing for their very powerful optimizing FORTRAN compiler. Duplication costs (for multiple systems) are one tenth of initial costs (for example, \$12,600 for the first minicomputer system, \$1260 for each next system.)

## 3.3 Comparison of Systems

The costs of the systems previously described are roughly equivalent. The 16 bit DATA GENERAL Eclipse S/250, DEC's PDP11/44, and the PERKIN-ELMER 3220 and 3240 are within the \$100K to \$200K range mentioned in the initial proposal. The PERKIN-ELMER 3240, while considerably more expensive than the other systems, has high speed capabilities approaching those obtainable with a third generation machine like the UNIVAC 1100/81. All four systems can perform the proposed regridding and mosaicking task within the time constraint if the approximate transformation is used for the major portion of the points as is currently done with the MARS system. The decision on which machine to choose should be based not only on the capability to perform the regridding and mosaicking task, but also on the capability to perform future tasks, the ease with which the system can be integrated into the existing DMA framework, and the reputation of the manufacturer(s) for delivery and support.

The DATA GENERAL S/250 is the same basic machine used in the UNAMACE equipment. As such, DMA has personnel who are familiar with the inevitable idiosyncrasies of a particular hardware system. However, the S/250 is only a 16 bit machine. Future work which DMA m ay desire to perform on the chosen system could possibly not be performed adequately on a 16 bit machine. On the other hand, since map oriented operations can quite often be realized as operations on matrices of elevation (or other) values, the built-in array processor of the S/250 could prove to be very useful for quick operations on a vector of values. The S/250 is a fast and powerful 16 bit minicomputer backed by a large experienced corporation.

The PERKIN-ELMER 3220 (or 3240) was designed as a scientific use 32 bit machine. Its instruction set and hardware configuration are oriented towards

manipulation of numerical data in an efficient manner. In addition the 3220 has a 32 bit architecture. Future DMA needs could be implemented on this machine with minimum modification. PERKIN-ELMER's optimizing FORTRAN compiler produces object code which approaches that of an experienced programmer. The "deluxe" 3240 minicomputer is the most powerful of the machines reviewed for this report. Its extremely high speed operations combined with a large memory address space would permit easy future software expansion according to DMA needs. FERKIN-ELMER is a large well known firm involved in many different fields.

DIGITAL EQUIPMENT's PDP11/44 (or similar models) are 16 bit minicomputers with general purpose instruction sets. The speed of this machine is adequate when an approximate transformation is used. Being one of the first minicomputers introduced, the PDP line has a proven architecture for a variety of tasks. In addition, the PDP is familiar to more programmers than the other machines, largely due to its presence at many universities. DEC is the largest minicomputer manufacturer and is known for its support services.

As this report was in the final stages of being written DEC announced a less expensive version of their VAX line of computers. The VAX is an extremely powerful 32 bit machine with a large memory address space. Before any decision is made on the type of machine to be used for the MiniMARS system we feel that this machine should be examined.

## 4. BENCHMARKS

The MiniMars algorithm relies on the ability of a minicomputer system to perform certain operations such that when comparisons are made the time required on a UNIVAC 1100/81 and the minicomputer are not radically different. With this requirement in mind, benchmark tests were performed on a UNIVAC and on four different minicomputers. Table 2 shows execution times for three different transformations performed on 10<sup>4</sup> points and the extrapolated time estimates for 10<sup>6</sup> points. The tests were performed on a UNIVAC 1108 and on a UNIVAC 1180. The minimal driver and transformation routines were then transported to a PDP11/45, P/E 3220 and 3240, and DG S/250 machines. Table 3 gives the times for 10<sup>4</sup> points and extrapolated values for 10<sup>6</sup> points. As can be seen, the times for the obsolete PDP11/45 are inadequate for rigorous transformation of all points of a model.

The PERKIN-ELMER machines show two times. These result from using a development compiler and an optimizing compiler. The times for the 3220 are within a factor of three of those of the UNIVAC 1100/81. The times for the 3240 are within a factor of two of those obtained from the UNIVAC systems, demonstrating the speed with which state-of-the-art minicomputers can perform. The lower estimate of the 3240 machine was obtained by using a compiler which places certain operations in writeable control store (in this case, sines and cosines). The use of microcoded instructions can increase performance by as much as 30%.

In order to test I/O speeds for disk accessing, a test was run on a PDP11/45 running Bell Laboratory's UNIX operating system. The disk used was an RKO5 equivalent with 70 ms average access time. This increase in access time over the proposed access time should be taken into consideration. Table 4 gives the results of 4 tests of pseudo-random reads of

Table 2.
Transformation Benchmarks For MiniMARS

	UNIVAC	1108	UNIVAC 1	100/81 *
Transformation	CPU Time for 10 <sup>4</sup> Pcints	Extrapolated 10 <sup>6</sup> Points	CPU Time for 10 <sup>4</sup> Points	Extrapolated 10 <sup>6</sup> Points
Geographic to	7.1 seconds	12 minutes	8.5 seconds	14 minutes
UNAMACE to Geographic	13.8 seconds	23 minutes	16.5 seconds	28 minutes
UNAMACE to UTM	20.1 seconds	35 minutes	24.6 seconds	41 minutes

\* -- These time were obtained while running the tests in "DEMAND" mode on the machine at DMAHTC. The algorithm used for computing execution time has been improved on the 1100/81. This probably accounts for the longer execution times than on the UNIVAC 1108.

	DATA	PERK	IN *	PERK	IN *	DEC
	GENERAL	ELM	ER	ELM	ER	PDP
	s/250	322	0	324	0	11/45
CPU Time for $10^4$ Points (seconds)	20	30	23	17.6	12.8	132
Extrapolated for 10 <sup>6</sup> Points (minutes)	33.3	50	36.3	28	21.3	220

\*-- Two times are shown for the Perkin-Elmer machines. The longer time in each case was obtained using a "development" compiler, the shorter time was obtained using an optimizing compiler.

The analysis in the original proposal used a range of 3 to 45 minutes for  $10^6$  points to be transformed. If rigorous ansformation is going to be used for each point only the PDP11/45 could not perform adequately.

10<sup>4</sup> 512 byte blocks. Table 5 contains the results of 4 tests of 10<sup>4</sup> sequential reads of 512 contiguous blocks. Projecting the timing values obtained into those possible with the specified high speed disk demonstrate that the I/O operations can be performed with sufficient speed, especially if there is concurrent input and output.

The benchmark tests have shown that current minicomputers do have the power and speed to compete with large main frames such as the UNIVAC 1100/81. The high reliability and low cost of minicomputers strongly suggest that they should be considered not only for the implementation of the algorithm in this report, but also for other algorithms performed by the MARS system. The following section gives recommendations on the implementation of this and other algorithms on both minicomputers and specialized hardware.

Table 4.
Random Reads from Disk

10000 random reads of 512 byte blocks RK equivalent disk with 70 msec avg. access PDP 11/45 under UNI X

Test #	# Users	wall clock time	user mode t1me	system mode time
1	>3	13 min 50 sec	4 sec	69 sec
2	l i l	11 min 30 sec	4 sec	68 sec
3	1 1	11 min 30 sec	4 sec	69 sec
4	1	11 min 29 sec	4 sec	66 sec
		1		

\* each of 4 tests read same pseudo-random sequence of 10000 blocks

Table 5.
Sequential Reads from Disk

10000 reads of contiguous 512 byte blocks, system environment as above

Test #	# Users	wall clock time	user mode time	system mode time
1 2 3 4	1 1 1	2 min 19 sec 3 min 4 sec 2 min 43 sec 2 min 41 sec	1 sec 1 sec 1 sec 1 sec	31 sec 31 sec 30 sec 30 sec

## 5. CONCLUSIONS AND RECOMMENDATIONS

## 5.1 General Conclusions

(G1) The MARS regridding step can be performed in a very simple manner as originally proposed, at a rate of  $10^6$  points in 40 to 80 minutes, and on hardware costing roughly \$125,000.

This conclusion is based on the decomposition of the processing into simple steps each one of which is tractable to analysis and can be calibrated by benchmarks. Actual benchmarks for I/O and computation, reported in Section 4, support the previous conclusion.

(G2) The current MARS software system could be transported to a minicomputer system with no loss in execution speed and a great saving in execution cost.

The minicomputers studied can have large memories and fast arithmetic and could easily host the current MARS. Throughput should increase if the system were dedicated to MARS through decreased overhead and I/O contention. Moreover, memory limitations are known to slow down the current UNIVAC MARS. Large memory increases possible in the mini systems could speed up the processing by reducing fragmentation. Costs of converting the current UNIVAC system would be high because of the complexity of that system - probably higher than the cost of creating the proposed Mini-MARS software system. Conversion of the current MARS was not actually a task of the current project, however, given the current information it is easy to evaluate such an option.

## 5.2 Conclusions Regarding Coordinate Transformations

(T1) Rigorous transformation of every grid point can double execution time relative to regridding with a large amount of interpolation.

This conclusion is based on data from the MARS system contained in the work proposal and confirmed by subsequent analysis and benchmarks. Actually, rigorous transformation creates a 50/50 mix of computation and I/O time. Minicomputers with slower arithmetic but comparably fast I/O would cause a strong shift toward being compute bound. See Appendix A for a study of the MARS transformation routines.

(T2) Rigorous transformation should be avoided on all systems

From T1 it is seen that even on very fast conventional computers (i.e. UNIVAC 1108, PERKIN-ELMER 3240) half of the process time will be taken up in transformation. Of the computers studied only the UNIVAC could meet the 80 minute process time if all points were regridded rigorously.

The PDP 11's would require several hours for rigorous transformation but could finish in less than 80 minutes using interpolation.

(T3) Provided that only 1 of 200 grid points were transformed rigorously all of the computers studied (PDP 11, S/250, UNIVAC 1108, 3220 and 3240) could regrid  $10^6$  points in less than 80 minutes.

This is a direct consequence of the analysis of the algorithms and the timings from Tables 2 and 3. Past experience with MARS indicates that the fraction 1 of 200 is very reason le; we will seldom have to rigorously transform more points than this.

(T4) At this point in time special off-the-shelf hardware to speed up the transformations does not appear to be cost effective.

The DG array processor, in the \$14,000 range, is the only inexpensive array processor available for any of the studied machines but it does not handle double precision and is not a true parallel processor. A recently announced Floating Point 64-bit array processor is in the \$150,000 - \$200,000 range. Since such a device could only half the computation time, for example on the PE3240, it would be wiser to double capacity by having two conventional systems. Future reductions in cost and interfacing problems would cause us to reconsider.

(T5) The costs of the 16 bit and 32 bit machines are close enough together that the selection of the 32 bit machine appears to be best. (This machine can be either the 3220 or 3240, or one not reviewed by L.N.K.).

The capability for future expansion and the easy addressing methods of the 32 bit CPU are very strong assets.

## 5.3 Final Conclusions

The Mini-MARS project can be implemented on a mini-computer. It is recommended that a 32 bit machine be selected. The MARS system even in its present form could be implemented on the same machine (as it now exists) with some increase in thru-put. Hardware costs will be in the proposed range of \$100K to \$200K. Setup and software costs should be within \$100K to \$200K.

APPENDIX A

## STUDY OF DMA TRANSFORMATION PACKAGE

The DMA coordinate transformation package contains several superb algorithms for performing coordinate conversion. Two subroutines, however, require modification in order to avoid possible incorrect computation. The suggested changes are given in Section A.

If a large set of points (10,000 points, for instance) are to be processed using the subroutines, some reduction in computation time can be achieved by avoiding recomputing constants such as  $\pi/2$ , the eccentricity of the spheroid, coefficients for equations, etc., in each call of a subroutine. The number of exponentiations, multiplications and divisions should be minimized. Specific suggested modifications in this direction are given in Section B. It should be pointed out that the saving in computation time using such modification is not likely to exceed 10%. On the otherhand, if such economization is combined with improvements in the computation of the trigonometric functions, the total saving in computing time can exceed 25%. In Section C, methods for reducing the computation time of the trigonometric functions are discussed. The actual FORTRAN package is given at the end of this memo.

## A. Corrections and Safeguard Steps

- 1. <u>FLHUPS</u>, line 9: Change "CON = 1.0" to "CON = 2.0DO".
  The derivation of the value for CON can be found in Adler ([1]), page 97.
- FLHUPS: Change all occurences of the FORTRAN library functions ABS, SIN, COS and SQRT, to DABS, DSIN, DCOS AND DSQRT, respectively. This is a precautionary step.
- 3. FLHXYZ, line 3: Change "C THIS PROGRAM TRANSFORMS GEOGRAPHIC COORDINATES
  TO LOCAL" to "C THIS PROGRAM TRANSFORMS GEOGRAPHIC COORDINATES TO
  GEOCENTRIC".

- 4. UPSFLH, line 10: Change "CON = 1.0" to "CON = 2.0D0".
- 5. UPSFLH: Change all occurences of the FORTRAN library functions ATAN, ABS, SIN, COS and SQRT to DATAN, DABS, DSIN, DCOS and DSQRT, respectively.
- 6. XYZFLH, line 28: The variable "A" should be assigned the correct value before this step is executed. Such an assignment step seems to be missing.

  Also the logic in the expression itself

$$FLH(3) = A - ABS(Z)$$

appears to contradict the definition of geographic coordinates (unless this is a special convention used at DMA). The formula one would generally use is

$$FLH(3) = DABS(Z) - AXES(2)$$
.

7. <u>UTMFLH</u>: The Newton iteration loop (lines 33-37) should contain an accuracy check in order to (i) alert the user to possible inaccurate results, and (ii) eliminate unnecessary loops when an accurate result has been obtained. See lines 47-50 of UPSFLH for an example of such a checking device.

- B. Reducing Computation Time (Economization of Arithmetric Operations)
  - 1. In an initialization subroutine, initialize PI and PIHALF:

PI = 3.141592653589793D0

PIHALF = PI/2.0D0

Save the results in a COMMON area.

Change every occurence of "PI/2.0" to "PIHALF":

line 14 of FLHUPS,

line 51 of UPSFLH,

lines 21, 25, 27, 30 of XYZFLH.

2. In an initialization subroutine, compute the eccentricity E and its square E2:

C A is semi-major axis and B is semi-minor axis

A = ....

 $B = \dots$ 

E2 = (A + B)\*(A - B)/A/A

E = DSQRT(E2)

Save the values of E and E2 in a COMMON area.

Remove lines 12, 13 of FLHUPS,

line 30 of FLHUTM,

lines 12, 13 of FLHXYZ,

lines 25, 26 of UPSFLH,

line 20 of UTMFLH,

line 41 of XYZFLH.

- 3. In an initialization subroutine, compute the coefficients A, B, C and D (lines 32-35 of FLHUTM). Save the results in a COMMON area. E and E2 should be computed before computing A, B, C and D.
- 4. Change lines 19-21 of FLHUPS to

TEMPL = (1.0D0 - E)/(1.0D0 + E)

R = CON\*(A/B)\*TANZ\*A\*(TEMP\*TEMPL)\*\*EX.

Change line 43 of UPSFLH to

TEMP2 = TEMP1/TEMP.

In each case, an exponentiation operation is eliminated. Exponentiation is costly: approximately eight multiplications are necessary to perform an exponentiation operation.

5. In UPSFLH, replace lines 34 and 35 with

$$S2 = 2.0D0 * S1 * C1$$

$$C2 = 2.0D0 * C1 * C1 - 1.0D0.$$

This modification eliminates one call of the function DSIN(P) and one call of the function DCOS(P).

6. In XYZFLH, add the line "RXY = X\*X + Y\*Y" after the line 42.

Change line 45 to "R = RXY + ZP\*ZP", and change line 54 to "R = RXY".

## C. Computation of Trigonometric Functions

In many subroutines, the time required to compute the trigonometric functions is significant. As a measure of this segment of computing time, we estimate the ratio R:

R = (Total number of multiplications and divisions necessary to compute the trigonometric functions in subroutine)/(Total number of multiplications and divisions performed in each call of the subroutine)

If a DO-loop is to be executed in the subroutine, the ratio R takes into account only the operation counts involved in one loop. The ratio will decrease somewhat if more than one loop is considered. The economization modifications of Section B are assumed.

Fortran trigonometric functions are usually implemented using Chebyshev polynomials or Lagrange interpolation polynomials. An example of an approximating polynomial for  $\cos \frac{1}{8}\pi x$  is

$$.9999999724 - .3084242527 x^2 + .0158499130 x^4 - .0003188790 x^6$$
,

Fike ([2]), page 133. In this case, four multiplications are performed during the evaluation of the polynomial using the factored form  $a + ((b + (c + dx^2)x^2)x^2) with a, b, c, d$  as above.

SUBROUTINE	R (approximate)
FLHUPS	50%
FLHUTM	33%
FLHXYZ	50%
LCGO	0%
(LCGO calls FLHXYZ and ORTM6A)	
MOVE	0%
(MOVE is called by TRANCD only)	
TRANCD	0%
(TRANCD is an administrative subrou	tine. It calls other
subroutines.)	
UPSFLH	35%
UTMFLH	40%
XYZFLH	20%

The above ratios justify considering "hard-wiring" the trigonometric functions, implementing faster piecewise polynomial approximations.

Note the following computation times cited for DSIN along with the source.

 $25 \times 10^{-6}$  second DG S/250 Eclipse with microcoded functions. Timing gotten from technical literature.

 $40 \times 10^{-6}$  second Univac 1108. Timing gotten from actual benchmark

program run.

97 x 10<sup>-6</sup> second Perkin Elmer 3220. Timing gotten from technical

literature.

Benchmarks actually run with  $10^4$  points transformed from geographic to UTM coordinates are as follows.

7.1 sec Univac 1108

23.0 sec Perkin Elmer 3220

12.8 sec Perkin Elmer 3240

## D. Documentation

Specific source-references should be given for the approximation formulas in <u>FLHUTM</u> and <u>UTMFLH</u>, since the formulas in the two subroutines are modifications of the original defining equations of the UTM coordinates.

## REFERENCES

- [1] Adler, R.K., Richardus, P., <u>Map Projections for Geodesists, Cartographers</u>
  <u>and Geographers</u>, North-Holland Publishing Company Amsterdam, American
  Elsevier Publishing Company, Inc., U.S.A. and Canada, 1972.
- [2] Fike, C.T., Computer Evaluation of Mathematical Functions, Prentice-Hall,
  Inc., Englewood Cliffs, N.J., 1968.

## DMA TRANSFORMATION SOFTWARE

Following is a listing of all transformation software currently in use by DMA. Line numbers in these listings are those referenced in the prior text. Four driver programs are listed before the subroutines in the package. These drivers, perhaps with some changes in constants, were used to run benchmarks on the transformation software. Benchmarks were run on two different Univac installations (1110 and 1180) and two different Perkin Elmer installations (3220 and 3240).

```
000001
            000
                   C BRIVER TO CAL! TRANCB FOR GEOGRAPHIC TO UTN CONVERSION
                   C THIS DRIVER SHORT CUTS BY NGT CALLING ROUTINE TRANCD****
000002
            000
                   C ALSO WRITTEN 'UNIVAC FREE' TO GO TO PERKIN-ELHER FOR BENCHMARK
000003
            000
000004
            000
                   C
000005
            000
                         IMPLICIT INTEGER(A-Z)
000006
                         DOUBLE PRECISION PTIN(3), PTOUT(3), DAXES(2), PO(3), HO, FLAG, ZONE, DPI
            000
000007
                         BOUBLE PRECISION F(4)
            000
800000
            000
                   C
                         KOUNT = 0
000009
            000
                         DPI = 3.14159265358979324D0
000010
            000
000011
            000
                         PTIN(1) = 10.*DPI/180.
000012
            000
                         PTIN(2) = 10.*BPI/180.
                         PTIN(3) = 0.0D0
000013
            000
000014
            000
                         DAXES(1) = 6378135D0
000015
            000
                         DAXES(2) = 6356750.52D0
000016
                   C CODE ADDED TO SHUNT CALL TO TRANCD
            000
000017
                         F(3)=DAXES(1)
            000
000018
            000
                         F(4)=BAXES(2)
000019
                         PO(1) = 10.000
            000
000020
            000
                         PO(2) = 20.*DPI/180.
000021
             000
                         PO(3) = 100.*DPI/180.
000022
            000
                         HB = 0.000
                         FLAG = 0.0D0
000023
            000
000024
            000
                         ZONE = 0.0DO
000025
            000
                         KFLAG = 7
                         DO 50 I = 1.200
000026
            000
000027
             000
                         DO 50 J=1,50
000028
             000
                         PTIN(1) = PTIN(1)+1.*DPI/180.
000029
            000
                         PTIN(2) = PTIN(2)+1.*BPI/180.
000030
            000
                         PTIN(3) = PTIN(3)+1.
000031
            000
                         KOUNT = KOUNT + 1
000032
            000
                   C
                         CALL TRANCD(PTIN, PTOUT, DAXES, PO, HO, FLAG, ZONE, KFLAG)
000033
                   C HERE IS CODE DONE IN TRANCD ENABLING THAT ROUTINE TO BE SHUNTED
            000
000034
            000
                         F(1)=PTIN(1)
000035
             000
                         F(2)=PTIN(2)
000036
             000
                         CALL FLHUTH(F, PTOUT, ZONE)
000037
            000
                         PTOUT(3)=PTIN(3)
000038
            000
                         IF (I.EQ.1.AND.J.EQ.1) WRITE(6,49) PTIN, PTOUT
000039
                         IF(I.EQ.200.AND.J.EQ.50) WRITE(6,49) PTIN, PTOUT
            000
000040
            000
                   49
                         FORMAT( PTIN ',3D20.10,/, PTOUT ',3D20.10,//)
000041
            000
                   50
                         CONTINUE
000042
            000
                         WRITE(6,100)KOUNT
000043
            000
                   100
                         FORMAT('ONORMAL EXIT, COUNT = ',16)
000044
            000
                         STOP
000045
            000
                         END
```

```
C DRIVER TO CALL TRANCD FOR UNAMACE TO GEOGRAPHIC CONVERSION
1
2
3
              IMPLICIT INTEGER(A-Z)
              DOUBLE PRECISION PTIN(3), PTOUT(3), DAXES(2), PO(3), HO, FLAG, ZONE, DPI
 5
        C
6
              KOUNT = 0
7
              PTIN(1) = -5000.000
              PTIN(2) = -5000.000
8
9
              DAXES(1) = 6378135D0
              BAXES(2) = 6356750.5200
10
              DPI = 3.14159265358979324D0
11
              PO(1) = 0.0
                              PLATITUBE
12
              PO(2) = 20.*DPI/180.
                                        <u>QLONGITUDE</u>
13
14
              PD(3) = 100.*DPI/180.
                                       BAZIMUTH
              HO = 0.000
15
              FLAG = 0.000
16
              ZDNE = 0.0D0
17
                              @ FOR UNA TO GEO
18
              KFLAG = 16
19
              DO 50 I = 1,10
20
              PTIN(3) = 0.0D0
              PB(1) = PB(1)+5.*DPI/180.
21
              DO 50 J = 1,10000
22
              PTIN(1) = PTIN(1)+1.
23
              PTIN(2) = PTIN(2)+1.
24
25
              PTIN(3) = PTIN(3)+1.
26
              KOUNT = KOUNT + 1
27
        50
              CALL TRANCD(PTIN, PTDUT, DAXES, PO, HO, FLAG, ZONE, KFLAG)
28
              WRITE(6,100)KOUNT
        100
              FORMAT('ONORMAL EXIT, COUNT = ',16)
29
30
              STOP
              END
31
```

```
C DRIVER TO CALL TRANCD FOR UNAMACE TO UTH CONVERSION
2
              IMPLICIT INTEGER(A-Z)
              DOUBLE PRECISION PTIN(3), PTOUT(3), DAXES(2), PO(3), HO, FLAG, ZONE, DPI
5
        C
              KOUNT = 0
              PTIN(1) = -5000.000
              PTIM(2) = -5000.0D0
              DAXES(1) = 6378135D0
10
              BAXES(2) = 6356750.52D0
              DPI = 3.14159265358979324D0
11
12
              PO(1) = 0.0
                               PLATITUDE
              PO(2) = 20.*DPI/180.
                                        QLONGITUDE
13
14
              PO(3) = 100.*DPI/180.
                                        PAZINUTH
              HO = 0.0D0
15
              FLAG = 0.0D0
16
17
              ZONE = 0.0D0
18
              KFLAG = 17
                              P FOR UNA TO UTH
              D0 50 I = 1.10
19
              PTIN(3) = 0.000
20
21
              PO(1) = PO(1)+5.*DPI/180.
22
              D0 50 J = 1,10000
23
              PTIN(1) = PTIN(1)+1.
              PTIN(2) = PTIN(2)+1.
24
25
              PTIh(3) = PTIN(3)+1.
26
              KOUNT = KOUNT + 1
              CALL TRANCD(PTIN, PTOUT, DAXES, PO, HO, FLAG, ZONE, KFLAG)
27
        50
              WRITE(6,100)KOUNT
28
29
        100
              FORMAT('ONORMAL EXIT, COUNT = ', 14)
30
              STOP
              END
31
        C DRIVER TO CALL TRANCD FOR GEOGRAPHIC TO UTH CONVERSION
 2
        C
 3
               IMPLICIT INTEGER(A-Z)
               DOUBLE PRECISION PTIN(3), PTOUT(3), DAXES(2), PO(3), HO, FLAG, ZONE, DPI
        C
               KOUNT = 0
             7P:IN(1) = 10.*DPI/180.
 7
 8
              PTIN(2) = 10.*DPI/180.
 9
              PTIN(3) = 0.0D0
10
               DAXES(1) = 6378135D0
11
               DAXES(2) = 6356750.52D0
12
              √DPI = 3.14159265358979324D0
13
              PO(1) = 10.0D0
                                   PLATITUDE
14
              PO(2) = 20.*DPI/180.
                                        PLONGITUDE
15
              PO(3) = 100.*DPI/180.
                                        HTUMIZAS
              HO = 0.0B0
17
              FLAG = 0.0D0
18
               ZONE = 0.0DO
                             P FOR GEO TO ITT
19
               KFLAG = 7
20
              B0 50 I = 1,2000
21
              D0 50 J = 1.50
22
              PTIN(1) = PTIN(1)+1.*DPI/180.
23
              PTIN(2) = PTIN(2)+1.*DPI/180.
24
              PTIN(3) = PTIN(3)+1.
25
              KOUNT = KOUNT + 1
26
        50
               CALL TRANCD(PTIN, PTOUT, DAXES, PO, HO, FLAG, ZONE, KFLAG)
27
               WRITE(6,100)KOUNT
        100
              FORMAT('ONORMAL EXIT, COUNT = ',16)
28
29
               STOP
30
              END
```

The second second

```
SUBROUTINE FLHUPS (PTIN, PTOUT)
                                                                                    FLH00100
        C
                                                                                    FLH00200
 3
        C THIS ROUTINE GEOGRAPHIC COORDINATES TO UNIVERSAL POLAR STEREOGRAPHIC
                                                                                   FLH00300
                                                                                    FLH00400
 5
               INPLICIT DOUBLE PRECISION (A-H,O-Z)
                                                                                    FLH00500
              DIMENSION PTIN(5), PTOUT(2)
                                                                                    FLH00600
7
        C
                                                                                    FLH00700
 8
              PI = 3.141592653589793
                                                                                    FLH00800
              CON = 1.0
9
                                                                                    FLH00900
10
              A = PTIN(4)
                                                                                    FLH01000
11
              B = PTIN(5)
                                                                                    FLH01100
12
              E = 1. - (B/A) * *2
                                                                                    FLH01200
13
              E = SQRT (E)
                                                                                    FLH01300
              P = PI/2.0 - ABS (PTIN(1))
14
                                                                                    FLH01400
              TANZ = SIN (P/2.0) / COS (P/2.0)
15
                                                                                    FLH01500
              COSP = COS (P)
                                                                                    FLH01600
16
              TEHP = (1. + E + COSP) / (1. - E + COSP)
17
                                                                                    FLH01700
18
              EX = E/2.
                                                                                    FLH01800
19
              TANZ = TANZ * TEMP**EX
                                                                                    FLH01900
20
              TEMP = (1. - E) / (1. + E)
                                                                                    FLH02000
21
              R = CON + (A/B) + TANZ + A + TEMP**EX
                                                                                    FLH02100
22
              PTOUT(1) = R + COS (PTIN(2)) + 2000000.0
                                                                                    FLH02200
23
              Y = R * SIN (PTIN(2))
                                                                                    FLH02300
24
                                                                                    FLH02400
              IF (PTIN(1)) 10,20,20
25
           10 \text{ PTOUT}(2) = 2000000.0 + Y
                                                                                    FLH02500
26
              60 TO 30
                                                                                    FLH02600
27
           20 \text{ PTOUT}(2) = 2000000.0 - Y
                                                                                    FLH02700
28
           30 RETURN
                                                                                    FLH02800
29
              END
                                                                                    FLH02900
```

## FLHUTM 1 of 2

```
SUBROUTINE FLHUTH (F.O.ZONE)
2
              GEOGRAPHIC TO UTH
3
              IMPLICIT BOUBLE PRECISION (A-H,L-Z)
              DIMENSION F(4), O(2)
5
        C
            F AND O ARE THE SAME CALLING VARIABLES THAT APPEAR IN GENCOR
        C
           F(1) (OR L1) IS THE LATITUDE IN RADIANS
            F(2) (OR L2) IS THE LONGITUDE IN RADIANS
8
            F(3) (DR A1) AND F(4) (OR B1) ARE THE AXES OF THE SPHEROID. A1 GT B1.
              L1=F(1)
10
              L2=F(2)
11
              A1=F(3)
12
              B1=F(4)
13
              Z = ZONE
        C Y IS A CONVERSION FACTOR DEG TO RAD
15
              Y=.0174532925199432958D0
16
              IF (ZONE.6T.60.0D0) ZONE = 0.0B0
17
              LONG = L2/Y
              IF (LONG.LT.-180.0D0) LONG = LONG + 360.0D0
18
              IF (LONG. 6T. 180. 0B0) LONG = LONG - 360. 0D0
19
20
              L2 = LONG + Y
21
              IF (ZONE.LE.O.ODO) 60 TO 1
                                               QZONE NOT YET COMPUTED
22
       C
       C CHECK FOR ZONE OVERLAP ON EITHER SIDE OF 180/-180 DEGREES
23
24
       C LONGITUDE. FORCE CONSISTENT LONGITUDE VALUE.
25
       C
              IF (LONG.LT.O.ODO.AND.ZONE.EQ.60.ODO) LONG = LONG + 360.ODO
26
              IF (LONG.GT.O.OBO.AND.ZONE.EQ.1.OBO) LONG = LONG - 360.ODO
27
                                       PRECOMPUTE L2 FOR OVERLAP
28
              L2 = LONG + Y
29
            E IS THE ECCENTRICITY SQUARED
       C
30
              E=(A1-B1)+(A1+B1)/A1/A1
          A, B, C, D DEPEND ONLY ON E AND ARE AS IN THE WRITE UP
31
32
              A=1.+E+(.75+E+(0.703125D0+E+.68359375D0))
              B=E+(0.375+E+(0.46875+E+0.512953125D0))
33
              C=E+E+(.05859375D0+E+.1025390625D0)
34
35
              D=E+E+E+0.01139322916666667B0
              C1=DCOS(L1)
34
37
               S1=DSIN(L1)
              T=DTAN(L1)
38
39
              $2*C1*C1*E/(1.-E)
40
              T2=T+T
```

## FLHUTM 2 of 2

```
41
            N IS THE RADIUS OF CURVATURE IN THE PRIME VERTICAL
42
              N=A1/DSQRT(1.-E+S1+S1)
              C3=1.-T2+S2
43
              C4=T+(5.-T2+S2+(9.+4.+52))
44
              C5=5.+T2+(T2-18.)+S2+(14.-58.+T2)
45
46
              C6=T+(61.+T2+(T2-58.)+S2+(270.-330.+T2))
47
              IF (ZONE.GT.O.ODO) 60 10 3
                                              PFORCE PREVIOUS ZONE
48
              IF (L2.6E.0.0) 60 TO 2
49
          Z IS THE ZONE
50
              Z=30.+DINT(LONG/6.)
51
              IF (Z.EQ.0.0D0) Z = 60.0D0
                                              QFOR -180 DEGREES LONGITUDE
52
              60 TO 3
53
              Z=31.+DINT(LONG/6.)
54
            M IS THE CENTRAL MERIDIAN IN RADIANS
55
        3
              M = (6.*Z - 183.) *Y
            S IS THE ARC LENGTH ALONG THE CENTRAL MERIDIAN
56
57
              S=A1+(1.-E)+(A+L1-B+DSIN(2.+L1)+ C+DSIN(4.+L1)-D+DSIN(6.+L1))
58
              D2=(L2-M)+C1
59
              D3=D2+D2
            CHECK TO AVOID UNDERFLOW
60
61
              IF (ABS(D2).LT.1.0E-5) 60 TO 10
                       W*D2*(1.+D3*(C3/6.+D3*C5/120.))*.9996D0
62
              M2=.9996D0+S+.9996D0+N+D3+(.5+T+D3+(C4/24.+D3+C6/720.))
63
64
              60 TO 20
65
        10
              E2=
                       N+D2+(1,+D3+C3/6,)+.9996D0
              N2=.9996D0+S+.9996D0+N+B3+T+.5
66
67
        20
              E2=E2+5.D5
88
              IF(N2.GE.O.) GO TO 30
69
              N2=N2+1.B7
70
            O(1) (OR E2) IS THE UTH EASTING
            Q(2) (OR N2) IS THE UTH NORTHING
71
        C
72
        30
              0(1)=£2
73
              G(2)=N2
74
              IF (ZONE.6T.O.ODO) 60 TO 899
75
              20NE = 2
        899
76
              RETURN
77
              END
```

```
FLH00100
               SUBROUTINE FLHXYZ(FI,X,AXES)
                                                                                    FLH00200
        C
 2
                                                                                    FLH00300
        C THIS PROGRAM TRANSFORMS GEOGRAPHIC COORDINATES TO LOCAL
 3
                                                                                     FLH00400
 4
                                                                                     FLH00500
               IMPLICIT DOUBLE PRECISION (A-H, 0-Z)
 5
                                                                                     FLH00600
               BIMENSION FI(3),X(3),AXES(2)
 6
                                                                                     FLH00700
        £
 7
                                                                                      FLH00
               SINFI = DSIN (FI(1))
 8
                                                                                      FLHOO
              COSFI = DCOS (FI(1))
 9
                                                                                      FLH00
               SINL = BSIN (FI(2))
10
                                                                                      FLH00
               cosi = Bcos (FI(2))
11
                                                                                     FLH01200
               ALFA = (AXES(2)/AXES(1))**2
12
                                                                                     FLH01300
               E2 = 1. - ALFA
13
                                                                                     FLH01400
               GAMA = 1. - E2*(SINFI**2)
14
                                                                                      FLHO
               GAMA = DSQRT (GAMA)
15
                                                                                     FLH01600
               FN = AXES(1)/GAMA
16
                                                                                     FLH01700
               GAMA = (FN+FI(3)) * COSFI
17
                                                                                     FLH01800
               X(1) = GAMA + COSL
18
                                                                                     FLH01900
19
               X(2) = GAMA * SINL
                                                                                     FLH02000
               \chi(3) = (FN * ALFA + FI(3)) * SINFI
20
                                                                                     FI H02100
               RETURN
21
                                                                                     FLH02200
               END
22
 1
               SUBROUTINE LCGO(PIN, POUT, AXES, ORIG, HO, NODE)
                                                                                     LCG00100
                                                                                     LCG00200
 3
        C THIS PROGRAM TRANSFORMS COORDINATES FROM LOCAL TO GEOCENTRIC AND VICE LCG00300
        C VERSA
                                                                                     LCG00400
 5
        C
                                                                                     LCG00500
        C MODE = 1 , GEOCENTRIC TO LOCAL
 6
                                                                                     LC600600
 7
        C MODE = 2 , LOCAL TO GEOCENTRIC
                                                                                     LCG00700
 8
                                                                                     LCG00800
 9
               IMPLICIT DOUBLE PRECISION (A-H.O-Z)
                                                                                     LCG00900
10
               DIMENSION PIN(3), POUT(3), AXES(2), ORIG(3), RT(3,3), PO(3)
                                                                                     LCG01000
        C
11
                                                                                     LCG01100
12
               POUT(1) = DRIG(1)
                                                                                     LC601200
13
               POUT(2) = ORIG(2)
                                                                                     LCG01300
14
               POUT(3) = HO
                                                                                     LC601400
              CALL FLHXYZ(POUT, PO, AXES)
15
                                                                                    LCG01500
16
               CALL DRIMGA(DRIG,RT)
                                                                                    LCG01600
17
               80 TO (10,30), MODE
                                                                                    LCG01700
           10 DO 20 I = 1,3
18
                                                                                    LCG01800
19
              POUT(1) = 0.0
                                                                                     LC601900
20
              B0 20 J = 1,3
                                                                                    LCG02000
              POUT(I) = POUT(I)+RT(I,J)+(PIN(J)-PO(J))
21
                                                                                    LCG02100
22
           20 CONTINUE
                                                                                    LCG02200
23
               60 TO 50
                                                                                    LCG02300
24
           30 \ DO \ 40 \ I = 1.3
                                                                                    LCG02400
25
              POUT(I) = PO(I)
                                                                                    LC802500
              BO 40 J = 1,3
26
                                                                                    LCG02600
              POUT(I) = POUT(I)+RT(J,I)+PIN(J)
27
                                                                                    LC602700
28
           40 CONTINUE
                                                                                    LCB02800
29
           50 RETURN
                                                                                    LCG02900
30
              END
                                                                                    LCG03000
```

```
M0U00100
              SUBROUTINE HOVE(A,B,N)
                                                                                   M0V00200
2
                                                                                   M0V00300
3
        ε
                                                                                   M8V00400
              IMPLICIT DOUBLE PRECISION (A-H,0-Z)
4
                                                                                   M8V00500
5
        C
                                                                                   MDV00400
6
        C
                                                                                   #DV00700
7
        C
                                                                                   00800VON
8
        C
              DIMENSION A(1),B(1)
                                                                                   MOV00900
9
                                                                                   M0V01000
              DO 10 I = 1,N
10
           10 B(I) = A(I)
                                                                                   MBV01100
11
                                                                                   MDV01200
              RETURN
12
                                                                                   M0V01300
              END
13
```

```
DRT00100
              SUBROUTINE ORTHAA(V,A)
                                                                                  DRT00200
 2
              IMPLICIT DOUBLE PRECISION (A-H.O-Z)
                                                                                  DRT00300
 3
              DIMENSION V(3),A(3,3),C(3),S(3)
                                                                                  ORT00400
        C
                                                                                  DRT00500
 5
              D0 10 I = 1,3
                                                                                  ORT00600
 7
              C(I) = COS(V(I))
                                                                                  DRT00700
           10 S(I) = SIN (V(I))
 8
                                                                                  DRT00800
 9
              A(1,1) = S(3)*S(1)*C(2) - S(2)*C(3)
                                                                                  DRT00900
10
              A(1,2) = S(3)*S(1)*S(2) + C(2)*C(3)
                                                                                  ORTO1000
11
              A(1,3) = -S(3)*C(1)
                                                                                  ORT01100
12
              A(2,1) = -C(3)+S(1)+C(2)-S(2)+S(3)
                                                                                  DRT01200
              A(2,2) = -C(3)*S(1)*S(2) + C(2)*S(3)
.13
                                                                                  DRT01300
              A(2,3) = C(3)*C(1)
                                                                                  BRT01400
14
15
              A(3,1) = C(1)*C(2)
                                                                                  ORT01500
                                                                                  ORT01600
              A(3,2) = C(1)*S(2)
16
17
              A(3,3) = S(1)
                                                                                  ORT01700
18
              RETURN
                                                                                  DRT01800
19
              END
                                                                                  ORT01900
```

The second secon

```
SUBROUTINE TRANCD (R.S.SEMI.P.HO.FLAG, ZONE, KFLAG)
                                                                                   TRA00100
        C
                                                                                   TRA00200
              IMPLICIT DOUBLE PRECISION (A-H.O-Z)
                                                                                   TRA00300
              DIMENSION R(3),S(3),P(3),F(6),SEHI(2),RP(3)
                                                                                   TRA00400
                                                                                   TRA00500
        C KFLAG DETERMINES THE FORM OF THE OUTPUT AND INDICATES THE FORM OF
                                                                                   TRA00600
        C THE INPUT. THE POSSIBILITIES ARE AS FOLLOWS
                                                                                   TRA00700
        C KFLAG=1 MEANS UTH TO GEOGRAPHIC
 8
                                                                                   TRA00800
              =2 MEANS UTM TO BEOCENTRIC
                                                                                    TRA00900
              =3 HEANS UTH TO LOCAL RECTANGULAR
10
        C
                                                                                    TRA01000
11
        C
              =4 MEANS UPS TO GEOGRAPHIC
                                                                                    TRA01100
12
        C
              =5 MEANS UPS TO GEOCENTRIC
                                                                                    TRA01200
                                                             TRANCD
13
              =6 MEANS UPS TO LOCAL RECTANGULAR
                                                                                   TRA01300
        C
14
        C
              =7 MEANS GEOGRAPHIC TO UTM
                                                                                    TRA01400
                                                             part 1 of 2
15
              =8 MEANS GEOGRAPHIC TO UPS
                                                                                    TRA01500
              =9 NEANS GEOGRAPHIC TO GEOCENTRIC
16
        C
                                                                                    TRA01400
17
        C
              =10 MEANS GEOGRAPHIC TO LOCAL RECTANGULAR
                                                                                    TRA01700
18
              =11 MEANS GEOCENTRIC TO UTN
                                                                                    TRA01800
              =12 MEANS GEOCENTRIC TO UPS
                                                                                   TRA01900
19
        C
20
              =13 MEANS GEOCENTRIC TO GEOGRAPHIC
                                                                                    TRA02000
21
              =14 MEANS GEOCENTRIC TO LOCAL RECTANGULAR
                                                                                   TRA02100
              =15 MEANS LOCAL RECTANGULAR TO SECCENTRIC
                                                                                   TRA02200
22
        £.
23
              =16 MEANS LOCAL RECTANGULAR TO BEOGRAPHIC
                                                                                   TRA02300
24
25
        C
              =17 HEANS LOCAL RECTANGULAR TO UTH
                                                                                   TRA02400
26
        C
              =18 MEANS LOCAL RECTANGULAR TO UPS
                                                                                   TRA02500
27
                                                                                   TRA02600
        C
28
        C P(3x1) IS A VECTOR, (LATITUDE, LONGITUDE, AZIHUTH) OF THE LOCAL SYSTEM. TRAC2700
        C THE ALTITUDE OF THE LOCAL RECTANGULAR SYSTEM IS ZERO.
29
                                                                                   TRA02800
        C A AND B ARE THE MAJOR AND MINOR SEMIAXES OF THE SPHEROID.
                                                                                   TRA02900
30
31
        C FLAG = O. IF IN THE MORTHERN HEMISPHERE , =1 IN THE SOUTHERN
                                                                                   TRA03000
        C R AND S ARE THE INPUT AND OUTPUT COORDINATES, RESPECTIVELY
                                                                                   TRA03100
32
33
             Ε
                     X
                              LATITUBE
                                                                                   TRA03200
34
        C S= N
                OR = Y
                         OR = LONGITUDE
                                                 SIMILARLY FOR R.
                                                                                   TRA03300
35
                              ALTITUBE
                                                                                   TRA03400
        C
             Н
                     Z
                                                                                    TRA03500
36
                                                                                   TRA03600
37
              IF (KFLAG) 220,220,10
           10 IF (KFLAG-18) 20,20,220
38
                                                                                   TRA03700
39
           20 IF (KFLAG-6) 100,100,25
                                                                                   TRA03800
                                                                                   TRA03900
40
           25 FLAG = 0.0
              IF (KFLAG-7) 30,40,30
                                                                                   TRA04000
41
           30 IF (KFLAG-8) 60,40,60
                                                                                   TRA04100
42
                                                                                   TRA04200
43
           40 IF (R(1)) 90,100,100
44
           60 IF (KFLAG-11) 70,80,70
                                                                                    TRA04300
           70 IF (KFLAG-12) 100,80,100
45
                                                                                   TRA04400
           BO IF (R(3)) 90,100,100
                                                                                   TRA04500
46
47
           90 FLAG = 1.0
                                                                                   TRA04600
                                                                                   TRA04700
          100 CALL MOVE (R,RP,3)
48
49
              60 TD(1,1,1,2,2,2,3,4,5,5,6,6,6,7,8,8,8,8),KFLAG
                                                                                   TRA04800
                                                                                   TRA04900
50
51
        C UTH TO GEOGRAPHIC
                                                                                   TRA05000
                                                                                   TRA05100
52
                                                                                   TRA05200
            1 F(1) = RP(1)
53
              F(2)=RP(2)
                                                                                   TRA05300
54
55
              F(3)=ZONE
                                                                                   TRA05400
56
              F(4)=SEHI(1)
                                                                                   TRA05500
              F(5)=SEHI(2)
                                                                                   TRA05400
57
              F(4)=FLAG
                                                                                   TRA05700
58
                                                                                   TRA65800
              CALL UTHFLH (F,8)
59
              8(3)=RP(3)
                                                                                   TRA05700
40
41
              IF (KFLAG-1) 110,220,110
                                                                                   TRA04000
                                                                                   TRACATOO
          110 CALL MOVE(S,RP.3)
62
                                                         A-17
```

```
63
                                                                                      TRA06200
         C BEOGRAPHIC TO BEOCENTRIC
 44
                                                                                      TRA06300
                                                                                      TRA06400
 45
             5 CALL FLHXYZ (RP,S,SEHI)
                                                                                      TRA06500
 66
                                                                                      TRA06600
 67
               IF (KFLAS-2) 120,220,120
 48
           120 IF (KFLAG-5) 130,220,130
                                                                                     TRA06700
           130 IF (KFLAG-9) 140,220,140
                                                                                     TRA06800
 69
 70
           140 CALL HOVE (S,RP,3)
                                                                                      TRA06900
 71
                                                                                     TRA07000
72
         C GEOCENTRIC TO LOCAL RECTANGULAR
                                                                                      TRA07100
 73
                                                                                      TRA07200
             7 CALL LCGO (RP,S,SENI,P,HO,1)
                                                                                     TRA07300
74
                                                     TRANCD
75
               BO TO 220
                                                                                      TRA07400
 76
                                                                                      TRA07500
                                                     part 2 of 2
                                                                                      TRA07600
 77
         C UPS TO GEOGRAPHIC
                                                                                      TRA07700
 78
 79
             2 F(1)*RP(1)
                                                                                      TRA07800
                                                                                      TRA07900
               F(2)=RP(2)
 80
               F(3) = FLAG
                                                                                      TRA08000
 81
                                                                                      TRA08100
 82
               F(4) = SEHI(1)
 83
               F(5) = SENI(2)
                                                                                      TRA08200
 84
               CALL UPSFLH (F.S)
                                                                                      TRA08300
                                                                                      TRA08400
 85
               S(3)=RP(3)
                                                                                      TRA085C0
               IF (KFLAG-4) 110,220,110
 84
 87
                                                                                      TRA08600
                                                                                      TRA08700
         C GEOGRAPHIC TO UTH
 88
                                                                                      TRA08800
 89
                                                                                      TRA08900
 90
             3 F(1)=RP(1)
               F(2)=RP(2)
                                                                                      TRA09000
 91
 92
               F(3) = SENI(1)
                                                                                     TRA09100
                                                                                     TRA09200
 93
               F(4) = SEHI(2)
 94
                                                                                     TRA09300
               CALL FLHUTH (F,S,ZONE)
 95
               S(3)=RP(3)
                                                                                     TRA09400
               60 TO 220
                                                                                     TRA09500
 96
 97
                                                                                     TRA09600
                                                                                     TRA09700
 98
         C BEOGRAPHIC TO UPS
                                                                                      TRA09800
 99
                                                                                     TRA09900
100
             4 F(1)=RP(1)
                                                                                     TRA10000
101
               F(2)=RP(2)
               F(3) = FLAG
                                                                                     TRA10100
102
               F(4) = SEMI(1)
                                                                                     TRA10200
103
                                                                                     TRA10300
104
               F(5) = SEMI(2)
105
                                                                                     TRA10400
               CALL FLHUPS (F.S)
106
               S(3)=RP(3)
                                                                                     TRA10500
                                                                                     TRA10400
107
               80 TO 220
                                                                                     TRA10700
108
         C
109
         C BEDCENTRIC TO BEOGRAPHIC
                                                                                      TRA10800
                                                                                      TRA10900
110
111
             6 CALL XYZFLH(RP,S,SEMI)
                                                                                     TRA11000
                                                                                     TRA11100
112
               IF (KFLAG-13) 170,220,170
           170 IF (KFLAG-16) 180,220,180
                                                                                     TRA11200
113
           180 CALL MOVE (S.RP.3)
                                                                                      TRA11300
114
                                                                                      TRA11400
115
                IF (KFLAG-11) 190,3,190
                                                                                      TRA11500
116
           190 IF (KFLAG-12) 200,4,200
                                                                                      TRA11600
117
           200 IF (KFLAG-17) 4,3.4
                                                                                      TRA11700
118
                                                                                      TRA11800
119
         C LOCAL RECTANGULAR TO BEOCENTRIC
120
                                                                                      TRA11900
                                                                                      TRA12000
             B CALL LCGO (RP,S,SEHI,P,HO,2)
121
122
               CALL MOVE (S,RP,3)
                                                                                      TRA12100
                                                                                      TRA12200
123
                IF (KFLAG-15) 6,220,6
               RETURN
                                                                                     TRA12300
124
         220
                                                    A-18
125
               END
                                                                                      TRA12400
```

```
SUBROUTINE UPSFLH(PTIN, PTOUT)
                                                                                    UPS00100
                                                                                    UPS00200
 2
        C THIS SUBROUTINE TRANSFORMS UNIVERSAL POLAR STEREOGRAPHIC COORDINATES UPS00300
 3
        C TO GEOGRAPHIC.
                                                                                    UPS00400
 5
        C
                                                                                    UPS00500
              IMPLICIT DOUBLE PRECISION (A-H,0-Z)
                                                                                    UPS00600
              DIMENSION PTIN(5), PTOUT(2)
                                                                                    UPS00700
 8
        C
                                                                                    UPS00800
              PI = 3.141592653589793
 9
                                                                                    UPS00900
10
                                                                                    UPS01000
              CON = 1.
              IF(PTIN(3)) 20,10,26
                                                                                    UPS01100
11
           10 Y = 2000000. - PTIN(2)
12
                                                                                    UPS01200
                                                                                    UPS01300
13
              FACT = 1.0
14
              60 TO 30
                                                                                    UPS01400
15
           20 Y = PTIN(2) - 2000000.
                                                                                    UPS01500
                                                                                    UPS01600
16
              FACT = -1.0
                                                                                    UPS01700
           30 X = PTIN(1) - 2000000.
17
              PTOUT(2) = ATAN2(Y,X)
                                                                                    UPS01800
18
19
              IF (ABS (X) - ABS (Y)) 40,40,50
                                                                                    UPS01900
           40 R = Y / SIN (PTOUT(2))
                                                                                    UPS02000
20
21
              60 TO 60
                                                                                    UPS02100
           50 R = X / COS (PTOUT(2))
                                                                                    UPS02200
22
23
           60 A = PTIN(4)
                                                                                    UPS02300
24
              B = PTIN(5)
                                                                                    UPS02400
              E2 = 1. -(B/A)**2
25
                                                                                    UPS02500
26
              E = SQRT (E2)
                                                                                    UPSC 2600
27
              TEMP = (1. - E) / (1. + E)
                                                                                    UPS02700
28
              EX = E/2.
                                                                                    UPS02800
29
              TANZ = (R / A) * (B/A) / ((TEMP**EX) * CON)
                                                                                    UPS02900
30
              P = ATAN (TANZ) + 2.0
                                                                                    UPS03000
31
              D0 70 I = 1.10
                                                                                    UPS03100
              S1 = SIN (P/2.0)
32
                                                                                    UPS03200
              C1 = COS (P/2.0)
33
                                                                                    UPS03300
34
              S2 = SIN(P)
                                                                                    UPS03400
35
              C2 = COS(P)
                                                                                    UPS03500
              TEMP = (1. + E + C2) / (1. - E + C2)
                                                                                    UPS03600
36
              TANP = S1 / C1
                                                                                    UPS03700
37
38
              C = TANP * (TEMP**EX) - TANZ
                                                                                    UPS03800
                                                                                    UPS03900
39
              C12 = C1**2
              CONST = (1. - E * C2) **2
                                                                                    UPS04000
40
              TEMP1 = TEMP **EX
41
                                                                                    UPS04100
42
              EXX = EX - 1.
                                                                                    UPS04200
                                                                                    UPS04300
              TEMP2 = TEMP ++EXX
43
              CONST = (.5 * TEMP1/C12) - (E2 * TEMP2 * TAMP * 82 / CONST)
44
                                                                                    UPS04400
45
              BP = - C / CONST
                                                                                    UPS04500
              P = P + DP
                                                                                    UPS04600
46
              IF (ABS (BP) - .000000005) 80,80,70
47
                                                                                    UPS04700
           70 CONTINUE
                                                                                    UPS04800
48
                                                                                    UPS04900
49
              PRINT 1000
         1000 FORMAT (14H2 ERROR UPSFLH)
                                                                                    UPS05000
50
51
           80 PTOUT(1) = (PI/2. - P) * FACT
                                                                                    UPS05100
              RETURN
                                                                                    UPS03200
52
                                                                                    UPS05300
53
              END
```

```
SUBROUTINE UTHFLH(F,0)
              UTH TO GEOGRAPHIC
        C
              IMPLICIT BOUBLE PRECISION (A-H,L-Z)
              BIMENSION F(6),0(2)
            F AND O ARE THE SAME CALLING VARIABLES THAT APPEAR IN GENCOR
          F(1) (OR E1) IS THE UTH EASTING. F(2) (OR N1) IS THE UTH NORTHING
7
          F(3)
                (OR Z) IS THE ZONE
 8
                (OR A1) AND F(5) (OR B1) ARE THE AXES OF THE SPEROID. A1 GT B1.
          F(4)
 9
        C
                 (DR H) IS 1 OR O. 1 FOR THE SOUTHERN HENISPHERE. O FOR THE
10
           NORTHERN HENISPHERE
11
              E1=F(1)
              N1=F(2)
12
13
              Z=F(3)
              A1=F(4)
14
15
              $1=F(5)
16
               H=F(6)
17
            Y IS A CONVERSION FACTOR, DEG TO RAD
        C
18
              Y=.0174532925199432958D0
19
            E IS THE ECCENTRICITY SQUARED
20
              E=(A1-B1)+(A1+B1)/A1/A1
21
          A, B, C, B DEPEND ONLY ON E AND ARE AS IN THE WRITE UP
              A=1.+E+(.75+E+(0.703125D0+E+.68359375D0))
22
23
              B=E*(0.375+E*(0.46875+E*0.512953125D0))
24
              C=E+E+(.05859375B0+E+.1025390625B0)
25
              B=E+E+E+.011393229166666665D0
26
            E2 AND N2 ARE THE UNSCALED UTHS
27
              E2=(E1-5.D5)/0.9996D0
28
              N2=(N1-H+1.D7)/0.9996D0
29
        C
            M IS THE CENTRAL MERIDIAN IN RADIANS
30
              M=(6.+Z-183.)+Y
31
            THE NEXT & LINES CONTAIN THE NEWTON ITERATION TO COMPUTE THE FOOTPOINT LAT
32
              Q=N2/A1/(1.-E)/A
33
              DO 10 I=1.5
34
              G=N2-A1*(1.-E)*(A*Q-B*DSIN(2.*Q)+C*DSIN(4.*Q)-6.*D*DSIN(6.*Q))
              G1=-A1*(1.-E)*(A-2.*B*DCOS(2.*Q)+4.*C*DCOS(4.*Q)-6.*D*DCOS(6.*Q))
35
              Q=Q-6/61
36
37
        10
              CONTINUE
38
        C THE FINAL VALUE OF Q IS THE FOOTPOINT LATITUDE
39
              C1=DCOS(Q)
40
              S1=BSIN(Q)
              T=BTAN(Q)
41
42
              12=T#1
            N IS THE RADIUS OF CURVATURE IN THE PRIME VERTICAL OF THE FOOTPOINT
43
44
              N=A1/DSQRT(1.-E+S1+S1)
45
              S2=C1+C1+E/(1.-E)
              D2=E2/N
46
47
              B3=B2±B2
48
              L2=B2*(1.+D3*(-(1.+2.*T2+S2)/6.+D3*(5.+6.*S2+T2*(28.+8.*S2+24.*T2)
49
             2)/120.))/C1+M
50
              L1=Q+D3+T+(1.+S2)+(-.5+D3+(5.+S2+(1.-4.+S2)+T2+(3.-9.+S2))/24.)
            O(1) (OR L1) IS THE LATITUDE IN RAD
51
52
            O(2) (OR L2) IS THE LONGITUDE IN RAD
53
              0(1)=L1
54
              LONG = L2/Y
55
              IF (LONG.LT.-180.0DO) LONG = LONG + 360.0DO
              IF (LONG.ST.180.080) LONG = LONG - 360.000
56
57
              L2 = LONG + Y
58
              0(2)=L2
59
              RETURN
              END
                                    A-20
```

```
SUBROUTINE XYZFLH(XYZ,FLH,AXES)
                                                                                       XYZ00100
        C
                                                                                       XYZ00200
 2
        C THIS SUBROUTINE CONVERTS POINT COORDINATES FROM BEDCENTRIC TO
                                                                                       XYZ00300
 3
        C GEOGRAPHIC
                                                                                       XYZ00400
 4
 5
        C THE SUBROUTINE USES DOUBLE PRECISION ARITHMATICS
                                                                                       XYZ00500
                                                                                       XYZ00600
 6
        C
 7
        C SPECIFICATIONS
                                                                                       XYZ00700
 8
        C
                                                                                       XYZ00800
               IMPLICIT DOUBLE PRECISION (A-H, 0-Z)
 9
                                                                                       XYZ00900
               BIHENSION XYZ(3),FLH(3),AXES(2)
                                                                                       XYZ01000
10
               PI =3.141592653589793D0
11
                                                                                       XYZ010
12
        C
                                                                                       XYZ01200
13
               X = XYZ(1)
                                                                                       XYZ01300
               Y = XYZ(2)
                                                                                       XYZ01400
14
15
               Z = XYZ(3)
                                                                                       XYZ01500
16
        C
                                                                                       XYZ01600
17
        C COMPUTE LONGITUDE LANDA
                                                                                       XYZ01700
18
                                                                                       XYZ01800
                                                                                       XYZ01900
19
               IF (X) 50,10,60
            10 IF (Y) 20,30,40
                                                                                       XYZ02000
20
21
            20 \text{ FLH}(2) = -PI/2.0
                                                                                       XYZ02100
                                                                                       XYZ02200
22
               80 TA 80
                                                                                       XYZ02300
23
            30 \text{ FLH}(2) = 0.0
24
               IF (Z) 32,32,33
                                                                                       XYZ02400
            32 \text{ FLH(1)} = -PI/2.0
                                                                                       XYZ02500
25
26
               GO TO 34
                                                                                       XYZ02600
                                                                                       XYZ02700
27
            33 \text{ FLH}(1) = PI/2.0
                                                                                       XYZ02800
28
            34 \text{ FLH}(3) = A - ABS (2)
29
                                                                                       XYZ02900
               60 TO 120
                                                                                       XYZ03000
30
            40 FLH(2) = PI/2.0
                                                                                       XYZ03100
31
               60 TO 80
32
            50 CON = -PI
                                                                                       XYZ03200
                                                                                       XYZ03300
33
               60 TO 70
34
            60 COM = 0.0
                                                                                       XYZ03400
                                                                                        XYZOO
35
            70 \text{ FLH(2)} = \text{DATAN (Y/X)} + \text{CON}
                                                                                       XYZ03600
36
        C
37
        C COMPUTE LATITUBE PHI
                                                                                       XYZ03700
                                                                                       XYZ03800
38
                                                                                       XYZ03900
39
            80 A = AXES(1)
                                                                                       XYZ04000
40
               B = AXES(2)
                                                                                       XYZ04100
41
               E2 = 1. - (B/A) + 2
42
               T1 = E2 + Z
                                                                                       XYZ04200
                                                                                       XYZ04300
43
               DO 100 I = 1.10
                                                                                       XYZ04400
44
               ZP = T1 + Z
45
               R = (X**2 + Y**2 + ZP**2)
                                                                                       XYZ04500
               SIMPI = ZP / DSQRT (R)
                                                                                        XYZOO
46
47
               T2 = (A + E2 + SINPI) / DSQRT (1.0 - E2 + SINPI++2)
                                                                                        XYZ00
48
               D = DABS (T1 - T2)
                                                                                        XYZOO
                                                                                       XYZ04900
49
               IF (B-.005) 110,110,90
                                                                                       XYZ05000
50
            90 T1 = T2
51
           100 CONTINUE
                                                                                       XYZ05100
                                                                                       XYZ05200
                    WRITE (6,1000)
52
53
          1000 FORMAT (14H2 ERROR XYZFLH)
                                                                                       XYZ05300
                                                                                       XYZ05400
54
          110 R = X**2 + Y**2
               R =DSQRT (R)
                                                                                       XYZ050
55
56
               ZP = Z + T2
                                                                                       XYZ05600
               FLH(1) = BATAN (ZP/R)
                                                                                        XYZ00
57
               DN = A / BSQRT (1. - E2 + SINPI++2)
                                                                                       XYZ050
58
                                                                                       XYZ05900
59
               R = ZP / SINPI
                                                                                       XYZ06000
               FLH(3) = R - DN
40
                                                                                       XYZ06100
61
           120 RETURN
                                                                                       XYZ06200
               END
42
```

-semigraph a

APPENDIX B

1-DataGeneral

QUOTATION

QUOTATION NO 181830

PLEASE REFER TO THIS QUOTATION NO IN ALL CORRESPONDENCE AND ORDERS

Route 4 Westboro Massachusetta 01581

5p. +11-485 9100 TWX 710 390-0309

. LNK Corp.

TO:

• 4321 Hartwick Rd.

• College Park, MD 20740

• Attn: Russ Smith/Dr. Kanal

## NEAREST DGC SALES OFFICE

- 7927 Jones Branch Dr.
- McLean, VA 22102
- . 703/827-9600

## THANK YOU FOR YOUR INQUIRY. WE ARE PLEASED TO QUOTE AS FOLLOWS:

DATE 7/29	9/80	REFERENCE		FREIGHT CHARGES	C		CASH s on Approval credit Dept	FOB	POINT OF ORIGIN	
ITEM	QUANTITY	,	DESCRIPTION		TUNUT	MAINT TOTAL PRICE	LICT DOLCE	DISC %	UNIT NET PRICE	TOTAL
			DELUXE S25	<u>o</u>						
		(One dis	k, two tares	s, consol	e)					
1	1	8635-NB	S250 with memory (two interleaved	o-way			40,500	1.5	34,425.00	34,425.00
2	1	8641	High Speed ware float:				6,195	15	5,265.75	5,265.75
3	1	6026	800/1600 To Cont.	ape w/			15,500	15	13,175.00	13,175.00
4	1	6026	800/1600 A	dd-on Tap	е		11,300	15	9,605.00	9,605.00
5	1	8650-B	Dual Perip	heral Bay	5		2,600	NА	2,600.00	2,600.00
6	1	6067-N	50MB Disk	with Cont	}		19,800	15	16,830.00	16,830.00
7	1	6040	60 CPS Term	minal			2,650	15	2,252.50	2,252.50
		HARDWARE	TOTAL	- <b></b>				+		84,153.25
	<u> </u>									
									ļ	Ì

## ATTACHMENTS:

DGC Discount Agreement Form\_\_\_\_

DGC Program License Agreement Form 500

DGC Program Availability Schedule Form 501

DGC Maintenance Contract Form\_\_\_\_

THIS COUNTY IN SHALL REMAIN FRANTO BY DO DAYS FROM THE LATE MIRRIES THAT I WOULD BE AND BY STAN CHAREAL CORPORATION DGC PRIOR TO COME FRANCE OF MAD CORPORATION AND ANY CROPE PLACED AS A PESCAL HERSELF SHALL BE SHALL REMAINS AND CONTINUE THE SELFE STAND BE SHALL REMAINS ANY CONTRACT RESULTING FOR THIS CALLE STAND CONTINUE AND CONTRACT RESULTING FOR THIS CALLE BY A STAND CONTRACT RESULTING FOR THIS CALLE BY A DULY AUTHORIZED REPRESENTATIVE OF CONTRACT OF MAY OF THE THEMS AND CONTRACT OF MAY OF THE THEMS AND THE ATTACHED AGREEMENTS SHALL ON LEFFE. THE IN WRITING AND AGREED TO BY AN AUTHORIZED REPRESENTATIVE OF LOC LOT MAKES NO MAPARANTIES, EITHER EXPRESS OR IMPLIED, AS TO THE FIRMS SOF THE FROM TO SAULT OF THE AUTHORIZED REPRESENTATIVE OF LOC LOT MAKES NO MAPARANTIES, EITHER EXPRESS OR IMPLIED, AS TO THE FIRMSS OF THE FROM TO SAULT OF THE CUSTOMER.

Michael Zuckerman, Federal Acct. Mgr.

tmc

From No. 13000113-04



## QUOTATION CONTINUATION SHEET

QUOTATION NO 181830

PLEASE REFER TO THIS QUOTATION NO IN ALL CORRESPONDENCE AND ORDERS

PAGE OF

		<del></del>		T					TAGE OF	
CPU TYP		/29/80	BENCE	FREIGHT CHARGES						
ITEM	QUANTIT	<del></del>	DESCRIPTION	<del></del>	MTLY UNIT PRICE	MAINT TOTAL PRICE	UNIT LIST PRICE	DISC.	UNIT NET PRICE	TOTAL
		TO ADD	BURST MULTIPL	EXOR CHAN	Ţ.					
1	1	6067-HN	50MB Disk w (substitute model for 6 previous pa	this 067-N on			21,800	15	18,530.00	18,530.0
2	1	8642	Burst Multi Channel (ad model to pro page)	d this			3,150	15	2,677.50	2,677.50
		REVISED	TOTAL		ļ					88,530.75
								}		
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\*Model/Feature Defined in Data General Price List

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See Page 1 for Signature



## QUOTATION CONTINUATION SHEET

QUOTATION NO 181830

PLEASE REFER TO THIS QUOTATION NO IN ALL CORRESPONDENCE AND ORDERS

PAGE OF

ITEM Q	7/29	,								
			DESCRIPTION		MTLY /	TOTAL PRICE	UNIT LIST PRICE	DISC.	UNIT NET PRICE	TOTAL
		SUPER D	ELUXE							
		TO ADD	INTEGRAL ARRAY	PROCESS	<u>DR</u>					
1	1	8652B	I/O only mod	lule			900	15	765.00	765.00
2	1	8652-C	I/O system N	Module			900	15	765.00	765.00
3	1	8315	I/O Bus Repe	eater			1,200	15	1,020.00	1,020.00
4	1	8644	Integral Arı	ay Proce	ssor		14,595	15	12,405.75	12,405.75
5	1	8638	Writeable Co	ntrol st	re		4,200	15	3,570.00	3,570.00
		REVISED	TOTAL							107,056.50
į										
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\*Model/Feature Defined in Data General Price List

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See Page 1 for Signature

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## QUOTATION CONTINUATION SHEET

181830

PLEASE REFER TO THIS QUOTATION NO.

PAGE C

										PAGE OF	
CPU TYP		100.100	BEFERENCE		FREIGHT CHARGES						
ITEM	QUANTIT	/29/80	DESCRI	PTION	<u></u>	MTLY UNIT PRICE		UNIT LIST PRICE	DISC %	UNIT NET PRICE	TOTAL
			SOFTW	ARE		PRICE	PRICE		1		
1	1	3359	for E	clipse	, Softwar	e Su	bscr	tem (MRDOS iption Ser redit, ins	rvic		2,400.0
2	1	3374	Fort. credi servi	t, ins	timizing tallatior	Comp , so	iler ftwa	), one tra re subscri	ini bti	ng on	2,000.0
3		xxxx	Diagn	ostics							N/C
ĺ		All e	equipment	prices	are as p	er G	s-00	c-01911.			
		Sched	NK Corp de dule, a le orization	tter f	rom the (	bntr	tili acti	zing the E ng Officer	ede (G	ral Supply by't) in	
		cost	) configur ACE system	ations	. An 863	5-NA	(wi	thout inte	erle	(not lowest aving - B at lower	

\*Model/Feature Defined in Data General Price List

B-4

See Page 1 for Signature

O' HOME: 140

CUSTOMER COPY

LNK CORPORATION 4321 Hartwick R College Park, M	LNK CORPORATION 4321 Hartwick Road College Park, Maryland 20740	PERKIN-ELMER COMPUTER SYSTEMS DIVISION 1764 Old Meadow Lane	R STEMS adow L	DIVISION ane		2070-09-428A PLEASE REFER TO THIS QUOTATION NUMBER ON ALL CORRESPONDENCE AND ORDERS	THIS QUOTATION
)	• •	McLean, Vìrginia 22101	ginia	22101		DATE 1/26/81	1/26/81 4/26/81
PRODUCT	DESCRIPTION	UNIT LIST PRICE	ρ	TOTAL LIST PRICE	DISC	TOTAL NET PRICE	MAINTENANCE
M32-260	Model 3220 Package System includes: .3220 Processor with 524,288 bytes MOS Memory .8 sets of 16, 32 bit general registers .Power Pail/Auto Restart .Memory Access Controller .OS/32 Bootloader .Loader Storage Unit .System Console .Quantity three Video - Model 550 .3200 Selector Channel .2 Line Comm Mux .8 Line Comm Mux .1/0 Expansion Chassis .56" Beige Cabinet .MSM 80F Disc System with controller .67MB Formatted Fixed Media .9 Track, 800/1600 CPI 75 IPS Tape System with Controller and Cabinet .Memory Access Controller .Battery Backup	75,100.	П	75,100.	21	59,329.	783.
M46-691	MSM 80F Disc System with Controller 67MB Formatted Fixed Media	15,200.	н	15,200.	z (	12,008.	150.

ANTHORIZED REPRESENTATIVE THE CORPORATION COMPUTER OPERATIONS

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LNK Corporation	FROM	• • Perkin-Elmer •				2070-09-428A PLEASE REFER TO THIS QUOTATION NUMBER ON ALL CORRESPONDENCE AND ORDERS	8A THIS QUOTATION
						DATE	
						VALID UNTIL	
PRODUCT	DESCRIPTION	UNIT LIST PRICE	QTV.	TOTAL LIST PRICE	DISC.	TOTAL NET PRICE	MAINTENANCE
M46-495	Expansion Tape, 9 Track, 800/1200 CPI 75IPS with Cabinet	9,625.	н	9,625.	- 51	7,603.	100.
M32-004	Floating Point Hardware	5,600.		5,600.	- 21	4,424.	70.
M32-001	1,024 Bytes Cache Memory	3,500.		3,500.	21	2,765.	5.
M32-010	3200 Selector Channel	1,750.		1,750.	21	1,382.	15.
M46-221	CF 120 Matrix Printer	3,500.	н	3,500.	27	2,765.	50.
M46-233	CP 120 Printer Interface	.000		•006	21	711.	20.
	TOTAL		<del></del>			90,998.	1,053.

AUTHORIZED REPRESENTATIVE THE PERKYN ELMER CORPORATION CONPUTER OPERATIONS

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Attn: R	4321 Hartwick College Park, Maryland Attn: Russ Smith	Perkin-Eimer Corpora 1764 Old Meadow Lane Polk Bldg., Suite 1 McLean, Virginia 22	rr Cor Sait Suit ginia	Perkin-Elmer Corporation 1764 Old Meadow Lane Polk Bldg., Suite 1 McLean, Virginia 22102		2070-09-427 PLEASE REFER TO TI NUMBER ON ALL CO AND ORDERS 7/24/80	2070-09-427 PLEASE REFER TO THIS QUOTATION NUMBER ON ALL CORRESPONDENCE AND ORDERS DATE: 7/24/80
PRODUCT	DESCRIPTION	UNIT LIST PRICE	4	TOTAL LIST PRICE	DISC.	VALID UNTIL: 10/24/80 TOTAL NET PRICE MAINT	0/24/80
M32-401	Hardware:		-				
	Model 3242 Processor with\$24,288 bytes of MOS ECC memory. 180-264 volts, 47-63 Hz includes:			\$111,000	21%	\$ 87,690	720
	• Expansion to 16MB of real memory • 8 Sets of 16 32 bit general registers • Power fail auto restart • Loader storage unit • Universal Clock • OS/32 Bootloader • RKb 4-way set associative CACHE • Model 550 CRT • 2 Line Comm. Mux. • 3240 Power Supply • Two 56" Biege Cabinets	<b>10</b>			-		
M32-423	Floating Point Processor		-	\$ 9,500	21%	\$ 7,505	09
M32-425	2K Words of 3240 Writable Control Store W/development software on 1600 CPI Tape.			\$ 7,500	21%	\$ 5,925	40
M46-691	MSM 80F Disc System with Controller, Formatted 67 MB Fixed Media.	\$ 15,200	2	\$ 30,400	21%	\$ 24,016	150

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AUTORIZED REPRESENTATIVE
THE PERTY ELMER CORPORATION
COMPUTER OPERATIONS

			auoT/	QUOTATION				QUOTATION NUMBER	9 E A :
٤	• LNK Corporati • 4321 Hartwick • College Park,	LNK Corporation FROM 4321 Hartwick College Park, Maryland	• • •	Perkin-Elmer Corporation 1764 Old Meadow Lane Polk Bldg., Suite 1	Corp dow I Suite	oration ane		2070–09-427 PLEASE REFER TO THIS QUOTATION NUMBER ON ALL CORRESPONDENCE AND ORDERS	THIS QUOTATION
	• •		• •	McL <b>ean,</b> Virginia 22102	ulla	77107		7/24/80 DATE: 7/24/80 VALID UNTIL:	80 10/24/80
116.04	PRODUCT	DESCRIPTION		UNIT LIST PRICE	ΔTV	TOTAL LIST PRICE	DISC.	TOTAL NET PRICE	MAINTENANCE
5	M32-010	3200 Selector Channel	ψ,	\$ 1,750	7	\$ 3,500	21%	\$ 2,765	15
ø	M46-494	9 Track, 800/1600 CPI, 75 IPS Mag Tape System with Controller and Cabinet.	· · · · · · · · · · · · · · · · · · ·	\$19,100	-	19, 100	21%	\$15,089	140
_	M46-495	9 Track, 800/1600, 75 IPS Expansion Drive, W/Cabinet	<u>پ</u>	\$ 9,625		\$ 9,625	21%	\$ 7,603	100
∞	M46-221	CP 120 Matrix Printer	φ.	\$ 3,500	_	\$ 3,500	21%	\$ 2,765	20
6	M46-233	CP Printer Interface	\$	006	_	006 \$	21%		10
		Totals:				\$195,025		\$154,069	1,285
		SOFTWARE:							
10 122 13	S80-016-ABC S80-016-ABC S90-028-071	OS/32 FORTRAN VII FORTRAN Enhancement Package				009 \$ 6,000 \$		000°9 000°9 \$	
		Totals:				\$ 12,600	_+	\$ 12,600	+

AUTHANIZED REPRESENTATIVE
THE PERKIN ELMER CORPORATION
COMPUTER OPERATIONS

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INK Corporation	4321 Hartwick	College Park, Maryland	ı	Attn: Russ Smith
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QUOTATION NUMBER:	2070-09-424	PLEASE REFER TO THIS QUOTATION	AND ORDERS	
UOTATION	Perkin-Elmer Corporation	1764 Old Meadow Lane	Polk Bldg., Suite 1	McLean, Virginia 22102

QUOTATION

FROM

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1980	21,
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July	UNTIL
DATE	VALID

	TEM .	NUMBER	DESCRIPTION	UNIT LIST PRICE	QTY.	TOTAL LIST PRICE	DISC.	TOTAL NET PRICE	MAINTENANCE
	1	M32-401	Hardware: Model 3242 Processor with 524,288		-	000 1115	21%	\$ 87,690	720
-					 <del> </del> 		}		ì
			■ Expansion to 16MB of real memory						
			• 8 Sets of 16 32 bit general registers • Power fail auto restart	<b>v</b> i					
			<ul><li>Loader storage unit</li><li>Universal Clock</li></ul>						
B-			• OS/32 Bootloader						
			<ul> <li>8Kb 4-way set associative CACHE</li> <li>Model 550 CRT</li> </ul>						
			• 2 Line Comm. Mux.						
			• 3240 Power Supply • Two 56" Biege Cabinets						
	~	M32-430	1,048,576 Bytes MOS/ECC Memory		7	\$ 23,900	218	\$ 18,881	240
	m	M32-423	Floating Point Processor		1	\$ 9,500	218	\$ 7, 505	09
	4	M32-425	2K Words of 3240 Writable Control Store W/development software on 1600 CPI TAPE		т	\$ 7,500	218	\$ 5,925	40
	_								
	ς.	M46-691	MCM 80F Disc System with Controller, Formatted 67 MB Fixed Media.	\$ 15,200	7	\$30,400	218	\$ 24,016	150
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THE PERMY ELMER CORPORATION
COMPUTER OPERATIONS

INK Corporation 4321 Hartwick	College Park, Maryland
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	Perkin-Elmer Corporation	a		McLean, Virginia 22102	
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	JE J	1764 Old Meadow Lane	Polk Bldg., Suite l	Ħ.	
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QUOTATION	ĘŢ	764	췭	뒴	
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	ROM.				

	1980 80
1980	21,
21, 19	g
_	
DATE: July	

	TT BA	PRODUCT	DESCRIPTION	UNIT LIST PRICE	47.	TOTAL LIST PRICE	DISC.	TOTAL NET PRICE	MAINTENANCE
	9	M32-010	3200 Selector Channel	\$1,750	2	\$3,500	218	\$2,765	15
		7 M46-494	9 Track, 800/1600 CPI, 75 IPS Mag Tape System with Controller and Cabinet	\$19,100	Н	\$19,100	218	\$15,089	140
	<del></del>	M46-495	9 Track, 800/1600, 75 IPS Expansion Drive, W/Cabinet	\$9,625	-	\$ 9,625	218	\$ 7,603	100
B-10	<u> </u>	9 M46-221	CP 120 Matrix Printer	\$3,500	н	\$ 3,500	218	\$ 2,765	S
<del></del>	22	10 M46-233	CP Printer Interface	006	1	006	218		10
			Totals			\$218,925		\$172,950	1,525
			SOFTWARE:						
	222	S80-016-ABC S80-016-ABC S90-028-071	OS/32 FORTRAN VII FORTRAN Enhancement Package			000 \$ 6,000 \$ \$		000'9 \$ 000'9 \$	I I
	<u></u>		Totals			\$ 12,600		\$ 12,600	

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THE PERING ELMER CORPORATION
COMPITER OPERATIONS

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## QUOTATION

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## DIGITAL EQUIPMENT CORPORATION

PHONE AC 617 897-5111 TWX: 710-347-0212-CABLE: DIGITAL MAYN, TELEX 94-84-57

C-104-104-8062

PLEASE REFER TO THIS QUOTATION NO IN ALL CORRESPONDENCE AND ORDERS

DATE22	<u>Septemb</u> er, 1980
REFERENCE	<u>GS-00C-01892</u>
DISCOUNT A	GREEMENT NO

NEAREST DIGITAL SALES OFFICE

8301 Professional Place Landover, Maryland 20785

P	R	o	D	U	C1	ΓL	IN	Ε	С	o	D	E
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L nk Corporation 4321 Hartwick Rd

Suite 321

College Park, MD 20740

Attn: Russ Smith

THANK YOU FOR YOUR INQUIRY. WE ARE PLEASED TO QUOTE AS FOLLOWS

\_\_

ITEM	QTY	MODEL NO	DESCRIPTION	16.4	MONTHLY MAIN*	ADD DN INST UHG	DISC	UNIT PRICE	NET AMOUNT
1 23.4.56.78.9	1 1 1 1 1 1 1	11X44-CA LA38-HA FP11-F RJM02-AA RM02-AA TJE16-EA TE16-AE H9642-DB BA11-KW	256KB ECC MOS, H9642, TU.78, 120V DECwriter II FPP for 1144 67MB Disk & Controller 67MB Disk Drive 800/1600 bpi 45 ips tape dr. 800/1600 bpi,45ips tape drive Expansion Cabinet without end panels Expansion Box	*	\$142 \$ 16 \$ 16 \$ 170 \$140 \$147 \$104 N/C		Disc	\$ 27,700 \$ 1,700 \$ 3,100 \$ 25,700 \$ 19,300 \$ 20,200 \$ 12,800 \$ 1,300 \$ 3,200 \$ 60	NET AMOUNT
10 11 12		BCO3M-25 DL11-WE QJ737-AD	Null Modem Cable 1 EIA Async Line RT Clock RSX11-M		N/C \$ 6 \$210			\$ 820 \$ 7,800	
13 14	1	QP230-AD DD11-DK	Fortran IV/RSX 11M DD11-D, 2-SU for BA11-K		\$ 35 N/C			\$ 1,000 \$ 860	
			Subtotal: Less GSA Discount	ļ	į			\$125,540 \$ 18,831 \$106,709	-
							_		
This quotation shall remain firm for 60 days from the dath herior, unless modified in writing its Digital Equipment Corporation prior to be acceptance of your contract offer. This quotation is subject to credit approves and is governed by the Digital Equipment Corporation							SUB -	\$106,709.00	
tandar	d terms	and conditions of sale an	bearing on the reverse hereof and of the terms as noted above	200	attar hed	haret.		PILIC	1

1.4 Software consulting 2.4 Computer Special 3.4 DEC system 4.4 Digital Component 5.5 Discount agreement or resident ferms. Systems terms purchase and Group terms and or one identifiers. Systems terms purchase and Group terms and purchase and Digital Should as fined and Digital as fined in ablied in ablie

ESTIMATED DELIVERY SCHEDULE SUBSECT TO STORE AND THE		
QUOTATION PREPARED BY Dale Vogel	PAGE 1	of <u>1</u>

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## QUOTATION

## DIGITAL EQUIPMENT CORPORATION

QUOTATION NUMBER
C-104-104-8061
PLEASE REFER TO THIS QUOTATION NO IN

NE AC 617 897-5111 TWX 710-347-0212-CABLE: DIGITAL MAYN, TELE	X 94-84-57 REFERENCE
	DISCOUNT AGREEMENT NO
PRODUCT LINE CODE	NEAREST DIGITAL SALES OFFICE
O LNK Corporation 4321 Hartwick Rd. Suite 321 College Park, MD 20740	8301 Professional Place Landover, Maryland 20785
Attn: Russ Smith	_

## THANK YOU FOR YOUR INQUIRY, WE ARE PLEASED TO QUOTE AS FOLLOWS

*E N*	QTY	MODEL NO	DESCRIPT	ION	Terms *	MONTH; 1 MAINT	ADD On INCT CHO	0!S:	UNIT PRICE	NET AMOUNT
+	1	11/34A-YC	11/34A CPU, 256KB Serial Line Interf	• •					\$15,300	\$15,300
2	1	FF11-A	Floating Point Pro						\$ 2,900	\$ 2,900
	2	RJM02+AA	67MB Disk & Contro		ļ				\$24,000	\$48,000
Ø 1.4	1	LA3ô-HA	DECwriter II - RS2	132			[		\$ 1,700	\$ 1,700
5	ì	TJE16-EA	800/1600 bpi 45 ip	s tape drive					\$20,200	\$20,200
ć	1	TE16-AE	800/1600 BFI tape	Drive					\$12,800	\$12,800
~		H960-CA	Cabinet						\$ 1,575	\$ 1,575
ê.	2	E003M-25	Null Modem Cable						\$ 60	\$ 60
9	2	BA11-KE	Expansion Box		1				\$ 3,000	\$ 6,000
10	-	4J737-AD	RSX11M		1	1			\$ 7,800	\$ 7.800
11	~	.P230-AL	FORTRAN IV/RSX11M			l	1		\$ 1,000	\$ 1,000
	_		1 01/21221						Ψ 1,000	<b>4 1,000</b>
			TOTAL: (GSA) 15% Discount							\$117,335.00 \$ 17,600.25
i										\$ 99,734.75
								ı		
	aguite or spail remain from for 6 class trim the date herest unless modified in writing by Digital Edupment Corporation prior to								SUB TOTAL	
in uning tallow of your contract offer. This ignoration is subject to credit approval and is governed by the Digital Educament Corporation is during terms, and conditions of saw appearing on the reverse network and or the reverse so noted above, and attached hereto						br .	PLUS INSTALLATION			
Ship are consulting 2 * Computer Scientists Systems form and condition		turnic Systems	purchase and Group terms and		between purchaser and Digital as filled in above			İ	PLUS INSURANCE	
i- 11	one for a requestry formation of the UBPSE FORM (page 2 or this form and forward to your Digital Sure of the Asia of this formation of the guidation must be accepted at Digitals composite offices by a duly autil Digital Egisporial or poster impurance with the provided or properly white instraints and a charge of \$50 per 3				horized re	presentat	ve	NET TOTAL AMOUNT		

ESTIMATED DELIVERY SCHEDULE	SUBJECT TO MODIFICA	TION BY DIGITAL				_
	Dale Vogel		local		PAGE 1	0F <u>1</u>
		В-	12	-		